# Implementation of an Embedded Hardware Description Language Using Haskell

Nélio Muniz Mendes Alves (Universidade Federal de Uberlândia, Brazil nelio@comp.ufu.br)

Sérgio de Mello Schneider (Universidade Federal de Uberlândia, Brazil sergio.schneider@facom.ufu.br)

**Abstract:** This paper describes an ongoing implementation of an embedded hardware description language (HDL) using Haskell as a host language. Traditionally, "functional" HDL's are made using lazy lists to model signals, so circuits are functions from lists of input values to lists of output values. We use another known approach for embedded languages, in which circuits are data structures rather than functions. This style of implementation permits one to inspect the structure of the circuit, allowing one to perform different interpretations for the same description. The approach we present can also be applied to other domain-specific embedded languages. We provide an elegant implementation of memories and a set of new signal types.

**Key Words:** domain-specific languages, embedded languages, hardware description **Category:** B.5.2 B.6.3 D.3.2 I.6.2

## 1 Introduction

Building a domain-specific language from scratch can be a long task because it consists of dealing with many issues like designing syntax, scoping, type and module systems, and developing tools like parsers, compilers or interpreters. The embedded approach is, indubitably, a good way to describe and to implement domain-specific languages. Building a domain-specific "library" on top of a convenient general-purpose language, one can get rid of many design decisions, because the infrastructure of the *host* language is inherited, avoiding most of the issues above. Some performance is lost, but often it is not so important. Benefits and drawbacks of the embedded approach are found in [Hudak, 1998].

Functional languages have some advantages that make them well-suited for the design of domain-specific languages: strong typing, pattern matching, higherorder programming (first class functions), laziness and parametric polymorphism are key features that make the design very elegant and modular.

We focus on the domain of hardware description, which is the area we are working on at the present time. We consider this area an excellent case study because it explores many features concerning the embedded approach and also because descriptions can be "interpreted" in several ways (e.g. they can be simulated, translated to other HDLs or input to verification tools).

We have chosen Haskell to develop our work because it encompasses several desired features as mentioned above. For instance, we highlight its strong type system that catches as many errors as possible at compile time, and type classes that provide concise and generic circuit descriptions. There are some publications that show a more detailed discussion about choosing Haskell as a host language. Some examples are [Elliott, 1999, Launchbury et al., 1999]. Haskell has been also used to embed several other domain-specific languages, including other hardware description languages.

Although we focus in Haskell and in the hardware description domain, this paper gives a general idea on how to embed languages into a lazy, strongly typed functional language.

A simplified version of the language that is being developed is presented. The reader is supposed to be familiar with the functional programming paradigm and with the Haskell framework. If it is not the case, see [Thompson, 1999] for an introduction to Haskell and [Hudak et al., 1992] for details.

#### 1.1 Overview of the paper

First, we present some background in "functional" hardware description and motivation. Then, we show the difference between representing circuits as functions over lists and as data structures and explain why we have chosen the second option. Further, we show the implementation of the language and discuss about important subtles and why we prefer some decisions. Then, we cite related work and, finally, we present conclusions and future work.

## 2 Background and Motivation

Before we start showing the implementation of our hardware description language, let us outline a brief background in "functional" hardware description.

### 2.1 A simple sequential circuit

Consider the simple circuit in figure 1, where (a) shows the circuit as a black box and (b) shows it from the inside. This is a "high-level" diagram of a simple counter circuit with an input bit and a vector of bits as output, representing an integer number. It is controlled by a clock signal that is not represented in the diagram. Its meaning is: in the *i*th clock tick, if the input bit x is *False*, the output number is the same as the output number in the clock tick *i*-1. If x is *True* the output is increased by one. Thus, if the circuit receives the sequence

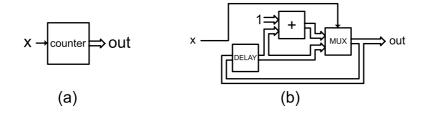


Figure 1: A simple counter example

[False, False, True, False, True, True] as input, it outputs the sequence of values [0, 0, 1, 1, 2, 3]. The *MUX* component is the same as an *if-else-then* function, + is the *plus* operation, and *DELAY* is an inherent sequential component that outputs its input value in the *i-1*th clock tick and, in case of the first clock tick, it outputs a given initial value as we shall see.

In the "functional" style of hardware description, the circuit in figure 1 would be described as a code like that of figure 2. Every circuit is represented by a

```
countWhen :: Signal Bool -> Signal Word8
countWhen x = out
where
out = mux x aux1 aux2
aux1 = delay 0 out
aux2 = plus (constant 1) aux1
```

Figure 2: Description of circuit in figure 1

function. A Signal models a wire in a circuit (or vector of wires – that is why the syntax of signal types is Signal XXX, where XXX says what kind of signal it is). As we are using Haskell, the first line is the function interface, which means that the circuit has a *boolean* signal as input and a word signal of eight bits as output. The next lines are the definition of the function (we like the clarity of the *where* construction). In the definition, we have to describe what each signal is. As the reader can see, if the designer has the diagram of the circuit, the description is straightforward. Note that delay receives an initial value 0 and an input value out. We are assuming that the definitions of mux, delay and plus are already provided by the basic library of the language. If there are some sub-circuits that are not provided by the basic library, they simply must be implemented as other functions.

## 2.2 Implementing a very simple language

A possible implementation of a very simple embedded language that permits describing the above counter is the library in figure 3 (note: we have already described the xor2 combinator because we will use it soon). Typically, such a

```
import Word
type Signal a = [a]
constant :: a -> Signal a
constant = repeat
plus :: Num a => Signal a ->
        Signal a -> Signal a
plus xs ys = zipWith (+) xs ys
mux :: Signal Bool -> Signal a ->
       Signal a -> Signal a
mux xs as bs = zipWith3 f xs as bs
  where f x a b = if x then b else a
delay :: a -> Signal a -> Signal a
delay x ys = x:ys
xor2 :: Signal Bool -> Signal Bool ->
        Signal Bool
xor2 xs ys = zipWith (/=) xs ys
```

Figure 3: Library for description in figure 2

library is composed by an abstract datatype (Signal a in this case), and combinators (plus, constant, mux, etc.) to produce larger sentences of the language. If we load this code together with the countWhen definition in a Haskell interpreter and run the command

Main> countWhen [False,False,True,False,True,True]

it will produce the result

[0,0,1,1,2,3]

as we expected. Often tools are implemented for interpreting the sentences, but in this example it is not the case, because circuits are Haskell functions. As we shall see, when implementing circuits as data structures, it will be necessary to implement interpretation functions because data structures are not naturally executable.

Another example is the circuit toggle in figure 4, composed by a xor2 component (the *xor* operation) and a delay. Its meaning is: For the *i*th clock tick (i > 1), if the *i*th input value is high, then the *i*th output value is the i - 1th output value inverted, else the *i*th output value is the same i - 1th value. The first output value is equal to the first input value.

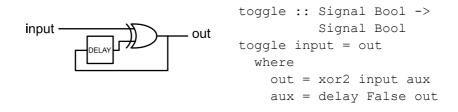


Figure 4: Diagram and description of the toggle circuit

Note that the definitions of the signals **out** and **aux** are mutually dependent. It is not a problem because of the lazy execution of Haskell and the initial value provided by the **delay** component. A mutually dependent definition without any **delay** would lead to an error (and smoke in a real circuit).

As we have mentioned, there is not explicit clock representation. It is a particular subtle in the "functional" style of hardware description: the notion of clock is implicitly carried by the position in the sequence of values (usually represented as ordinary lists). Thus, low-level details about timing are not considered: the simulation tools assume that the clock period is long enough to update all the internal component outputs. The careful reader probably has realized that "functional" HDL's fits well for signal processing, microarchitectures and the like.

## 2.3 Functions on lists vs. Data structures

In the previous subsection, we outlined an implementation of a simple embedded hardware description language as a library in which signals are modeled as lists and circuits are Haskell functions from lists to lists. With this implementation we can not do much more than simulate the circuits. We can not access the internal structure of the function to see how it was built. Therefore, we want to implement the circuits in such a way that we can inspect its internal structure and perform different interpretations like simulation, verification, translating to other languages and so on.

In figure 5 we sketch a simple implementation in which circuits are represented by a data structure (in this case, a tree). We are considering only boolean signals for now. Now the basic combinators are *signal expression builders* and the

data Signal	low = Bool False
= Bool Bool	high = Bool True
Var String	var x = Var x
Inv Signal	
Xor Signal Signal	inv x = Inv x
And Signal Signal	xor2 x y = Xor x y
Or Signal Signal	and $x y = And x y$
Delay Bool Signal	or2 x y = Or x y
deriving Show	delay x y = Delay x y

Figure 5: Representing signals as data structures

circuits are nothing more than bigger expressions. With this basic library, the style of descriptions remains the same, as we can see in the arbitrary example in figure 6. The functions low and high are primitive combinators to build "boolean"

Figure 6: Arbitrary circuit example

leaves" in the tree. The var combinator takes a string and builds a symbolic leaf in the tree (symbolic values are useful for performing interpretations like verification and translation to other languages). Figure 7 shows two examples of trees built from the circuit definition in figure 6. The first tree represents the circuit in some given boolean signals and the second represents the circuit in symbolic values. These expression trees now must be *interpreted*. Evaluating (or simulating) the expression represented by the tree in figure 7 (a) does not seem to be a complex task – a simple recursive traversing algorithm could do it. Also,

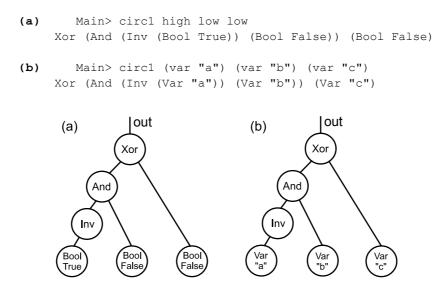


Figure 7: Data structures generated for real values and symbolic values respectively

suppose we want to traverse the tree in figure 7 (b) and generate code for the VHDL language. It would be carried out in a similar way.

However, the language presented is very poor because it cannot deal with primordial issues that must be treated. In the rest of the paper we show this issues and the solutions to solve them.

## **3** Implementation

## 3.1 Back to the parametric signal type

For performance and resource issues, we would like to abstract not only a single wire as a signal. We would like to represent a vector of eight bits as a signal of type Word8, a vector of sixteen bits as a signal of type Word16 and so on. Thus, we would like to come back to the parametric signal type Signal a.

To do this, we use the approach shown in [Leijen and Meijer, 2000]: we define an expression type Node encompassing all types and basic gates. Then, to prevent building incorrect sentences (e.g. *Xor (Bool False) (Word8 27)*) we define a layer of type safety (a *phantom type*) and build basic combinators respecting the signals types, as shown in figure 8 (data type) and figure 9 (some basic functions).

It is vital to provide function signatures in order to obtain type safety. As an example, if there was not a signature in the xor2 function, its type would be

```
data Node
 = Var String
  | Bool Bool
  | Word8 Word8
  | Word16 Word16
  | Inv Node
  | Xor Node Node
  | And Node Node
  | Or Node Node
  | Plus Node Node
  | Mux Node Node Node
 | DelayB
           Bool
                    Node
 | DelayW8 Word8 Node
  | DelayW16 Word16 Node
newtype Signal a
 = Signal Node
```

Figure 8: Implementing parametric signal type (data type)

## Signal $a \rightarrow Signal \ b \rightarrow Signal \ c.$

To save space, only a few combinators are shown in figure 9. Further we will implement some polymorphic combinators, like mux, var and plus. For now, we are assuming there is only a specific function for each type of signal: muxB is a multiplexor on single bits, muxW8 is a multiplexor on vectors of eight bits and so on. The same occurs for var, plus and delay.

#### 3.2 Detecting sharing

Let us consider the circuit in figure 10. As one can see, the result signal from the *and* gate is shared by the *xor* and the *or* gates. With the present implementation of the language, there is no way of building a traversing function that can detect such sharing. If one runs any traversing function for circ2 (varB "a") (varB "b") (varB "c"), such function would "understand" this sentence as a tree with redundant branches, as in Figure 11 (a). It would be worse if we call it for the toggle circuit in figure 4 because it would lead to an infinite tree! What we would like to get is a graph as in figure 11 (b).

To avoid performing redundant computations or incurring in an infinite loop, it would be necessary to give a unique *tag* to each node and also perform a convenient traversal algorithm on the new structure. In functional programming, it is very difficult to represent graphs with sharing without adding *impure* features. In [Claessen and Sands, 1999], Claessen and Sands show some previous solutions

```
low :: Signal Bool
low = Signal (Bool False)
w8 :: Word8 -> Signal Word8
w8 x = Signal (Word8 x)
xor2 :: Signal Bool -> Signal Bool -> Signal Bool
xor2 (Signal x) (Signal y) = Signal (Xor x y)
muxW8 :: Signal Bool -> Signal Word8 ->
        Signal Word8 -> Signal Word8 ->
        Signal Word8 -> Signal Word8
muxW8 (Signal c) (Signal x) (Signal y)
 = Signal (Mux c x y)
delayB :: Bool -> Signal Bool -> Signal Bool
delayB x (Signal y) = Signal (DelayB x y)
```

Figure 9: Implementing parametric signal type (some basic functions)

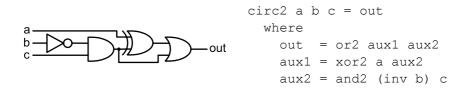


Figure 10: A circuit with a shared signal

and propose to solve this problem extending Haskell with reference types. The big advantage is that this technique keeps the clear and sweet style of description, without explicit naming or any other changes for the designer point of view. The major disadvantage of this technique is that it uses an impure mechanism to give unique names to the nodes, which loses referential transparency.

A referenced object of type Ref a is an object of type a "packed" together with an implicit unique *tag.* To build a reference type, there exists the function  $ref :: a \to Ref a$ . To "unpack" a reference type, there exists the function  $deref :: Ref a \to a$ . To compare if two references are the same, there exists the infix operator ( $\langle = \rangle$ ) ::  $Ref a \to Ref a \to Bool$ .

The final implementation of the signal type and some basic combinators are given in figure 12 (the data type) and figure 13 (some basic functions). The implementation of the *Ref* module can be found in [Claessen, 2001].

A new type **Graph** was created to not clutter up the definition of the Node type. The Node type defines all basic gates and end values that can appear in a

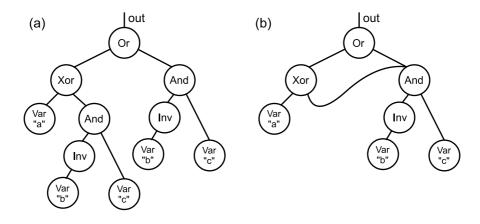


Figure 11: Tree with redundant information and graph with sharing

circuit description and the Graph type adds recursion and references.

#### 3.3 The BitVect class

We have implemented a *BitVect* type class to provide polymorphic combinators over different signal types (figure 14). We have implemented instances for *Signal Bool, Signal Word8*, etc. With this class, for example, any kind of multiplexor (on single bits, on vectors of eight bits, etc.), are represented by a function called mux. The same occurs for other combinators belonging to the class. The dff combinator is a circuit equivalent to a delay initialized with zero. We could not include delay in this class because of the fact that its initial value would have to be different for each instance.

With this class one can declare polymorphic circuits. Consider the above counter again. Now we can describe the same counter for any signal type as shown in figure 15. The type of the counter is now  $BitVect \ a \Rightarrow Signal \ Bool \rightarrow a$ . The Haskell type inference system is responsible for matching the correct instance class, depending on where the counter is inserted.

#### 3.4 Overloading tuples and lists of signals

Often, a circuit output contains more than one signal. In this case, they must be grouped in a tuple or list or a combination of them (because functions return only one value). Also, for overloading issues, we do the same (grouping in tuples and lists) for input values, as we have already done in figure 13. As a example, a *halfAdd* circuit that receives two bits and returns their sum and carry bit would have the signature *halfAdd* :: (*Signal Bool*, *Signal Bool*)  $\rightarrow$ 

```
import Word
import Ref
data Node a
  = Bool Bool
  | Word8 Word8
  | Word16 Word16
  | Var String
  | Inv a
  | Xor a a
  | And a a
  | Or a a
  | Plus a a
  | Mux a a a
  | DelayB Bool
                    a
  | DelayW8 Word8 a
  | DelayW16 Word16 a
newtype Graph
  = G (Ref (Node Graph))
newtype Signal a
  = Signal Graph
```

Figure 12: Adding references to the nodes (data type)

(Signal Bool, Signal Bool). Why have we grouped inputs and outputs together? Because we want to provide generic interpretation functions for the descriptions.

To help overloading tuples and lists of signals, we have implemented a Struct type and a *Generic* type class the same way in [Claessen, 2001] (figure 16). We created Gen instances for (), Signal a, Gen  $a \Rightarrow [a]$ , (Gen a, Gen  $b) \Rightarrow (a, b)$  and so on. Thus, every time we have to deal with a Generic type, we convert it to an object of type Struct Graph (using to), traverse it for every single value, then convert it again to the Generic type (using from).

Thus, a simulating function that receives a circuit and a list of inputs and returns a list of outputs would have the signature:  $sim :: (Gen \ a, Gen \ b) \Rightarrow (a \rightarrow b) \rightarrow [a] \rightarrow [b].$ 

#### 3.5 Memories

We have implemented memories in a similar way we have implemented delay: defining the initial value and input values. Suppose our language provides a readonly memory with 8-bit address and 16-bit values (figure 17 (a)), and a register

```
low :: Signal Bool
low = Signal (G (ref (Bool False)))
varB :: String -> Signal Bool
varB x = Signal (G (ref (Var x)))
xor2 :: (Signal Bool, Signal Bool) -> Signal Bool
xor2 (Signal x, Signal y) = Signal (G (ref (Xor x y)))
muxW8 :: (Signal Bool, (Signal Word8, Signal Word8))
            -> Signal Word8
muxW8 (Signal c, (Signal x, Signal y))
        = Signal (G (ref (Mux c x y)))
delayW8 :: Word8 -> Signal Word8 -> Signal Word8
delayW8 x (Signal b)
        = Signal (G (ref (DelayW8 x b)))
```

Figure 13: Adding references to the nodes (some basic functions)

file (note: we give a example of a simple register file, which writes a word and reads a word per cycle) with an 8-bit address, 16-bit values (figure 17 (b)). We put a new option in the Node type for each kind of memory the language will support and create basic combinators to build them (see figure 18. Although it seems quite simple to implement memories, the real work is in their simulation, where we use mutable arrays for better performance and to save resources.

#### 3.6 Interpretation tools

Suppose we have defined some circuit and want to simulate it. We have to implement a function that receives the circuit, a list of input values and then examines the graph corresponding to the circuit, evaluating it for each input value. We use the ST monad [Launchbury and Jones, 1995] because we want to perform destructive updates in the simulation.

As we have already mentioned, the simulation function has the signature:  $sim :: (Gen \ a, Gen \ b) \Rightarrow (a \rightarrow b) \rightarrow [a] \rightarrow [b].$ 

First, we traverse the circuit structure, converting reference types to "real" pointer references (mutable variables), using the function toSTRefs, which type is  $Struct Graph \rightarrow ST \ s \ (Struct \ (STS \ s))$ , where the  $STS \ s$  type is described in figure 19. This function traverses the circuit data structure keeping track of the sharing information and builds another data structure on top of the  $STS \ s$  type.

```
class BitVect a where
  zero :: a
 one
        :: a
 var
        :: String -> a
 plus :: (a,a) -> a
 dff
        :: a -> a
       :: (Signal Bool, (a,a)) -> a
 mux
instance BitVect (Signal Word8) where
  zero = w8 0
       = w8 1
 one
       = varW8
 var
 plus = plusW8
       = delayW8 0
 dff
 mux
       = muxW8
```

Figure 14: The BitVect class and an instance example

```
countWhen x = out
where
out = mux (x, (aux1, aux2))
aux1 = dff out
aux2 = plus (one, aux1)
```

Figure 15: Polymorphic counter

The  $STS\ s$  type defines all possible kinds of pointer references that might appear. The first kind (with the STT constructor) belongs to trivial gates (without internal state), the following three types belongs to delay components and the last to memories. Note that all types are ST references to tuples. In all cases, the first element is a recursive Node – that is exactly what we want to do because we are building another graph with ST references instead of Ref references. The second element is the present value of the Node in the simulation. For stateful components, there is a third element of the type of their internal state, that will be updated whenever necessary.

Further, we run a stateful algorithm to simulate the circuit, updating internal states and calculating output values. For performing other interpretations, a similar approach must be taken. For generating VHDL code, for example, its necessary to give a symbolic input to the circuit and perform a traversal al808 Alves N.M.M., de Mello Schneider S.: Implementation of an Embedded Hardware ...

data Struct a	class Gen a where
= Single a	to :: a -> Struct Graph
Compound [Struct a]	from :: Struct Graph -> a

Figure 16: The Struct type and Gen class

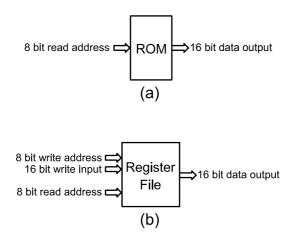


Figure 17: A read-only memory and a simple register file

gorithm that generates the corresponding string code depending on what each node is. We have not done it yet because we are still studying VHDL subset needed to represent our circuit elements.

## 4 Related Work

Embedding a domain-specific language into Haskell has been an interesting topic of research nowadays. Haskell has been successfully used to embed several applications such as 2D and 3D animation [Elliott, 1999], music [Hudak et al., 1996], SQL queries [Leijen and Meijer, 2000] and others.

Johnson's work "Synthesis of Digital Designs from Recursion Equations" [Johnson, 1984] and Sheeran's [Sheeran, 1983] " $\mu FP$ , an algebraic VLSI design language" have inspired many efforts in representing circuits by the functional-like style of description. Below, we cite the main works that have influenced our research:

The Hydra system [O'Donnell, 1996], developed by O'Donnell, consists of a set of methods and software tools for circuit design. It was previously built on top of the functional languages Daisy, Scheme and LML. Hydra provides some high-order combining forms and circuits are implemented as functions on stream

```
data Node a
= Bool Bool
 | Word8 Word8
 | Word16 Word16
 | Var String
 | Inv a
 | Xor a a
 . . .
 | RomW8xW16 [Word16] a
 | RegFileW8xW16 [Word16] a a a
rom8x16 :: [Word16] -> Signal Word8
           -> Signal Word16
rom8x16 ws (Signal x)
  = Signal (G (ref (RomW8xW16 ws x)))
regFile :: [Word16]
           -> ((Signal Word8, Signal Word16),
               Signal Word8)
           -> Signal Word16
regFile ws ((Signal a, Signal w), Signal r)
  = Signal (G (ref (RegFileW8xW16 ws a w r)))
```

Figure 18: Implementing memories

values. One of Hydra's strengths is simulation, and it has been used to teach computer architecture at undergraduate level at University of Glasgow.

Hawk [Matthews et al., 1998] is an embedded language for describing modern microarchitectures. The aim of Hawk is to provide clear and concise microprocessors specification (to achieve this, Hawk has a rich library of superscalar microprocessor elements and provides behavioral descriptions using *lifting* and concepts like *transactions*). Hawk permits one to perform simulation, verification and algebraic simplification. As far as we know, Hawk doesn't make VLSI synthesis or netlist generation.

Lava [Bjesse et al., 1998, Claessen, 2001], created by Bjesse, Claessen, Sheeran and Singh, provides a set of tools, which can perform interesting circuit interpretations, like simulation, verification and VHDL code generation for FPGA implementation. Like Hydra, Lava provides high-order combining forms. We have

Figure 19: The STS s type

been highly inspired by the Lava system, mainly by its signal representation and overloading tuples and lists [Claessen, 2001]. This work differs from Lava because (a) we provide other high-level gates for the descriptions (memories for example), (b) we are implementing our own interpretations for the descriptions and (c) we are making our own implementation for some aspects of the core of the language like (c.1) implementing delay differently (in Lava, the initial value of delay is a generic signal, but we implement it as a specific constant) and (c.2) providing several types of word signals (as far as we know, Lava provides only *Signal Bool* and *Signal Int*) and overloads them on some operations.

### 5 Conclusions and future work

We have embedded a domain-specific language for synchronous circuit design. We show that this implementation leads to a clear and concise style of description to the language user, and also to a reduced number of function names because of the type polymorphism. Much of the Haskell infrastructure like module system, reporting errors, syntax and scoping are inherited to the embedded language, which makes the language design time very much reduced. In few hours one can declare initial definitions and see the circuits running. It certainly could take a long time if designing the language from scratch. Our first contribution was to summarize in one paper all the crucial aspects of an implementation of an embedded language for hardware description.

We also contribute with a gentle way of representing memories, where the initial values of a ROM or a RAM are represented by a Haskell list and further executed as a lazy state array. This representation put together the facility of just declaring a list in a Haskell module, and the desirable destructive update (in the case, of course) execution by demand.

We are currently working on the interpretations of the descriptions. We traverse the data structure of the circuit calculating result values or reporting errors. We are studying the subset of VHDL and Verilog languages (the most widely used HDL's) for translating our descriptions into them. As we have mentioned, we already know the technique of translation, but we must know all the syntax needed to represent our circuit elements.

Also, we are exploring ways of implementing new computer architecture elements like shared buses. We have encountered some problems in our first implementation of shared buses, but we believe that it is not a big problem because we have implemented them in an alternative way (with circuits as functions on lazy lists) and they worked perfectly. They must be treated differently from other components because of the special semantics of the three state buffers.

We expect to apply optimizations on the descriptions using some techniques presented in [Elliott et al., 2000]. We also could think about increasing the performance using the strict state monad, but we would lose many desired features, specially working with infinite lists. If we used strict monad, it could not be performed:

#### Main> sim countWhen (repeat high)

Another future direction is to apply our descriptions to formal methods. The data structure of our descriptions is well suited and ready to apply verification algorithms. Lava and Hawk have already been used as verification tools, performing operations like testing properties, algebraic reasoning and theorem proving. We hope to apply operations like those in our circuit elements too.

#### References

- [Bjesse et al., 1998] Bjesse, P., Claessen, K., Sheeran, M., and Singh, S. (1998). Lavahardware design in Haskell. In International Conference on Functional Programming. ACM SigPlan.
- [Claessen, 2001] Claessen, K. (2001). Embedded Languages for Describing and Verifying Hardware. PhD thesis, Chalmers University of Technology and Göteborg University, Göteborg, Sweden.
- [Claessen and Sands, 1999] Claessen, K. and Sands, D. (1999). Observable sharing for functional circuit description. In Thiagarajan, P. S. and Yap, R., editors, Advances in Computing Science ASIAN'99; 5th Asian Computing Science Conference, volume 1742 of Lecture Notes in Computer Science. Springer Verlag.
- [Elliott, 1999] Elliott, C. (1999). An embedded modeling language approach to interactive 3D and multimedia animation. *IEEE Transactions on Software Engineering*, 25(3).
- [Elliott et al., 2000] Elliott, C., Finne, S., and de Moor, O. (2000). Compiling embedded languages. In Workshop on Semantics, Applications and Implementation of Program Generation.
- [Hudak, 1998] Hudak, P. (1998). Modular domain specific languages and tools. In Devanbu, P. and Poulin, J., editors, *Proceedings: Fifth International Conference on Software Reuse*. IEEE Computer Society Press.

- [Hudak et al., 1996] Hudak, P., Makucevich, T., Gadde, S., and Whong, B. (1996). Haskore music notation - an algebra of music. *Journal of Functional Programming*, 6(3).
- [Hudak et al., 1992] Hudak et al., P. (1992). Report on the programming language Haskell, a non-strict, purely functional language, version 1.2. ACM SIGPLAN Notices, 27(5). See http://www.haskell.org/definition for latest version.
- [Johnson, 1984] Johnson, S. (1984). Synthesis of Digital Designs from Recursion Equations. The ACM Distinguished Dissertations Series, The MIT Press.
- [Launchbury and Jones, 1995] Launchbury, J. and Jones, S. P. (1995). State in haskell. Lisp and Symbolic Computation, 8(4).
- [Launchbury et al., 1999] Launchbury, J., Lewis, J. R., and Cook, B. (1999). On embedding a microarchitectural design language within Haskell. In Proceedings of the fourth ACM SIGPLAN International Conference on Functional Programming. ACM Press.
- [Leijen and Meijer, 2000] Leijen, D. and Meijer, E. (2000). Domain specific embedded compilers. In 2nd USENIX Conference on Domain-Specific Languages, volume 35 of ACM SIGPLAN Notices. ACM Press.
- [Matthews et al., 1998] Matthews, J., Cook, B., and Launchbury, J. (1998). Microprocessor specication in Hawk. In *IEEE International Conference on Computer Lan*guages, Chicago, Illinois. IEEE Computer Society Press.
- [O'Donnell, 1996] O'Donnell, J. (1996). From transistors to computer architecture: Teaching functional circuit specification in Hydra. In *Functional Programming Languages in Education*, volume 1125 of *Lecture Notes in Computer Science*. Springer Verlag.
- [Sheeran, 1983] Sheeran, M. (1983).  $\mu FP$ , an algebraic VLSI design language. PhD thesis, Programming Research Group, Oxford University.
- [Thompson, 1999] Thompson, S. (1999). The Craft of Functional Programming. Addison Wesley, 2nd edition.