

CHAITIN'S TOYLISP ON A CONNEX MEMORY MACHINE ¹

Gheorghe Ștefan

Politechnical University of Bucharest, Department of Electronics, Bd. Armata
Poporului 1-3, Bucharest 6, Romania, email: stefan@hera.pub.ro.

Mihaela Malița

University of Bucharest, Faculty of Mathematics, Str. Academiei 14, Bucharest 1,
Romania, email: system@bsu.ro.

Abstract: This paper describes an implementation of Chaitin's ToyLisp [Chaitin '87] on a Connex Memory Machine (CMM) [Ștefan '85]. The Connex Memory Machine has a smaller complexity than previous Universal Machines used to run Lisp programs, so the time and space used in running Lisp programs can be considerably decreased. A ToyLisp like language can be used with a CMM to construct a Lisp (Co)Processor for accelerating Lisp processing in conventional architectures.

1 Introduction

Improving the performance of a string processing system could be done in two main ways:

- by defining and designing a high performance processing unit, having a “well fitted” set of functions, or
- by finding a “good” memory support for the data structures.

We have investigated the second alternative by defining a more “natural” memory support for lists, i.e. a better representation for storing and manipulating lists. We suggest a “smart memory”, in which some of its functions are performed at the storage level. Two main consequences derive from this approach:

- the processor attached to the memory becomes simpler and faster,
- the computational processes are simpler and their time and space complexities decrease.

In the '80s a small team in the Polytechnical University of Bucharest designed and implemented a Lisp Machine as a microprogrammed machine. From this experience a new memory model has emerged: the Connex Memory [Ștefan '85].²

Our paper has two aims:

¹ C. Calude (ed.). *The Finite, the Unbounded and the Infinite, Proceedings of the Summer School “Chaitin Complexity and Applications”*, Mangalia, Romania, 27 June – 6 July, 1995.

² Some applications of this memory were presented in [Ștefan '91], [Ștefan 95], [Hasci '95].

- a *theoretical* one: to offer another model for Universal Machine used to interpret Chaitin's ToyLisp;³
- a *practical* one: to define and implement a Lisp (Co)Processor starting from a ToyLisp like language as an assembly language.

2 Basic Requirements for String Processing

A Lisp-like language efficient implementation requires some unusual features, as:

- a “natural” representation of S-expressions on the physical support,
- a “natural” manipulation of S-expressions,
- time operation uncorrelated with the string length.

All these requirements can be satisfied with a physical support that:

- finds (accesses) the starting place of a substring in a string,
- inserts/deletes a symbol in an accessed point,
- delimits a self-delimited substring.

Dealing with symbols implies operations as finding, matching, inserting, deleting, moving, copying. These operations, usually, don't affect the symbol itself, but its position in the string. Memory functions are crucial in this case. Numerical operations are realized by functions that modify the value of their arguments using processing units. A processor like approach is more fitted for numbers.

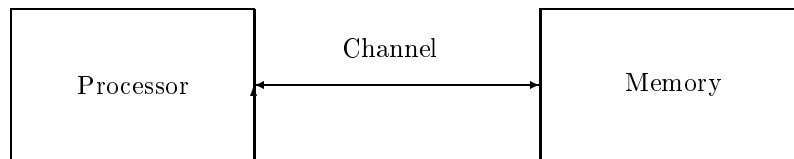


Fig. 1. The von Neumann Model

Having in mind the well known von Neumann model (Processor - Channel - Memory, see Fig. 1) we believe that for a more efficient symbol manipulation we need new memory functions instead of more powerful processors. Therefore, our proposal is a new concept of memory: the Connex Memory.

3 The Connex Memory

3.1 Informal Definition of the Connex Memory

The *connex memory* (CM) is a physical support for a symbolic string in which we can *find any substring*, identifying, in such a manner, any place in the string, for *reading*, *inserting* or *deleting* a symbol or a substring of symbols.

The content of the CM is a string of variables: $v_1 v_2 \dots v_i \dots v_n$. Each variable v_i has:

³ This could be a step towards obtaining a shorter diophantine equation describing Chaitin's Omega Number, [Chaitin '87, Calude '94].

- a *value* from a finite alphabet A ,
- a *state* which is marked or non-marked; the access point is at the first marked variable.

For example, the content in some place in CM is the string: ...(\hat{b} ubu (\hat{g} ood boy))... In Fig. 2 we can see the structure of the representation of the variables from the string: one bit for the marker and $m = \log_2(\text{card}(A))$ bits for each symbol in the alphabet A .

On any string stored in CM we can apply the set of functions described in the following definition.

Definition 1. The *connex memory* CM1 is a physical support for a string of variables, having values from a finite set of symbols A and two states: *non-marked* or *marked*, over which we can apply the following set of functions:

- *RESET* s : all the variables after the first marked variable take the value s
- *FIND* s : all the variables that follow a variable having the value s switch to the marked state and the rest switch in the non-marked state
- *C(onditioned)FIND* s : all the variables that follow a variable having the value s and being in the marked state switch in the marked state and the rest switch in the non-marked state
- *INSERT* s : the value s is inserted before the first marked variable
- *READ up|down|_* : the output has the value of the first marked variable and the marker moves one position to right (*up*) or to left (*down*) or remains unchanged (*_*)
- *DELETE* : the value stored in the first marked position is deleted, the position remains marked (the output has the value of the first marked variable) and the symbols from the right are moved one position left

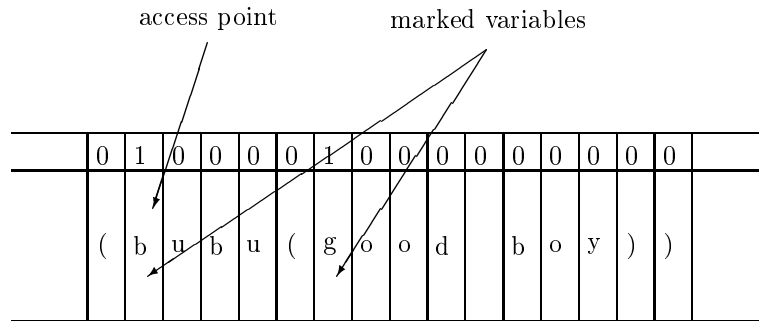


Fig. 2. The content of CM. An example

For different purposes in different stages of the computational process we need different types of markers. Until now our example has involved only one marker. We shall consider an extended definition of CM with two or more markers. In this way we could “colour” the symbols of the string with more than one “colour” (marker).

Definition 2. The CM2 has in addition to the set of functions defined in for CM1 (see Definition 1) the following new function:

SET POINTER $p_1|p_2|\dots|p_k$: the pointer p_i ($i = 1, 2, \dots, k$) is set to the first position of the marker and modifies the next functions as follows (the square brackets are used to indicate optional fields in the mnemonics of the function):

- *INSERT* $[p_i]$, s : inserts the symbol s in the position indicated by the pointer p_i ; if a pointer is not indicated, s is inserted to the first occurrence of the marker;
- *READ up|down|* – $[p_i]$: starts reading from the position indicated by the p_i pointer which is affected in the same manner as the marker;
- *DELETE* $[p_i]$: deletes the position pointed by p_i .

According to these definitions the CM is structured as a *bi-directional shift register* in which any significant point is *marked*, as a consequence of an *associative sequential mechanism* used to find a name in a number of steps equal to the length of the name. In the marked place, *read*, *insert* and *delete* can be performed. Theoretically, the CM at the right end is unlimited, and, consequently, can be used for simulating or emulating efficiently **any number of registers having an unspecified length** (theoretical infinite). Briefly: *CM* = is a *CAM* designed as a *Bi-directional Shift Register* left delimited by the *first marker*.

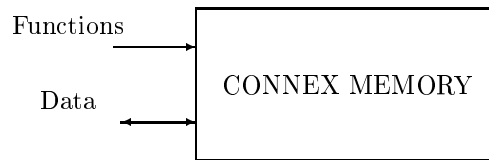


Fig. 3. Block Diagram of CM

The block diagram of CM1 from Fig. 3 shows the connections for data and functions defined before. We should not be surprised that this kind of memory *has no addresses*. Indeed, we don't need them because the access point is found by an associative search. In this way we avoid the \log_n connections used for addressing a standard memory.

It is a real joy to discover that this type of memory could remain, with an appropriate design, in the class of $O(n)$. At this reduced complexity, all functions are executed in time $T(n) \in O(1)$, in one clock cycle. For example, using the 16 Mb DRAM technology we realize our CM of 64 Ksymbol, where each symbol is encoded in 12 bits with 4 markers (having 16 states per symbol).

3.2 The Connex Memory at Work

Let us see some examples illustrating the main abilities of the CM.

Example 1. Using the CM1 we can find any substring in a string. Suppose that we have in a CM the following string:

...(bubu (bad butcher))...(bulgaria(...))...

and we want to select and read the list of *bubu*'s properties, i.e., *(bad butcher)*. The following sequence of functions is executed:

```

FIND (
CFIND b
CFIND u
CFIND b
CFIND u
CFIND blank
loop
  READ up
  until )
repeat

```

The content of the CM becomes successively (the marked places are indicated by oversigned symbols):

```

...(^bubu (^bad butcher))...(sup>^bulgaria (...))...
...(^bubu (^bâd butcher))...(sup>^bûlgaria (...))...
...(^bu^bu (^bad butcher))...(sup>^bu^lgaria (...))...
...(^bubu^ (^bad butcher))...(sup>^bulgaria (...))...
...(^bubu^ (^bad butcher))...(sup>^bulgaria (...))...
...(^bubu (^bad butcher))...(sup>^bulgaria (...))... / out = ( /
...(^bubu (^bâd butcher))...(sup>^bulgaria (...))... / out = b /
...(^bubu (^ba^d butcher))...(sup>^bulgaria (...))... / out = a /
...(^bubu (^bad^ butcher))...(sup>^bulgaria (...))... / out = d /
and so on, until:
...(^bubu (^bad butcher))...(sup>^bulgaria (...))... / out = ) /.

```

Example 2. Let us suppose that we want to change the first property of *bubu* with the value *good*. The sequence of functions will be:

```

FIND (
CFIND b
CFIND u
CFIND b
CFIND u
CFIND blank
READ up
loop
  DELETE
  until blank
repeat
INSERT g
INSERT o
INSERT o
INSERT d
INSERT blank

```

Now the new content of the CM becomes:

```

...(^bubu (^good butcher))...(sup>^bulgaria (...))...

```

4 CM Machine as a Universal Machine

The Connex Memory Machine (CMM) has the computational power of a Universal Turing Machine. In order to compare the CMM with other models we will make a short review of two other models: Universal Turing Machine (UTM) and Chaitin's Register Machine (RM).

4.1 Universal Turing Machine

Instead of the classical definition for a Turing Machine (TM) with:

- an infinite tape containing a string of symbols that can be read or modified,
- a finite automaton (which, for UTM, "knows" how to interpret a symbolic substring on the tape as a TM description),
- a read/write head which accesses the tape,

we propose a TM version more appropriate to the actual technology. In Fig. 4 the UTM contains:

- an infinite Random Access Memory (RAM), instead of the tape
- a finite automaton, as interpreter for TM description from the RAM
- an up-down counter that generates the address to the RAM.

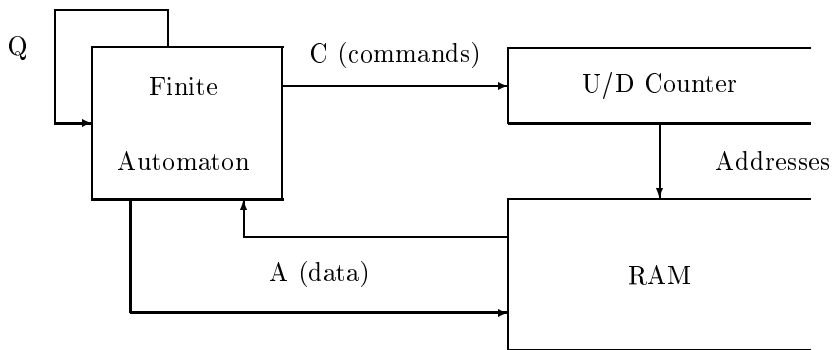


Fig. 4 Universal Turing Machine (UTM)

Definition 3 An UTM is a 4-tuple (Fig. 4):

$$UTM = (A, Q, f; \#)$$

where:

- A, the finite alphabet (for the RAM),
- Q, the finite set of states (of the automaton),
- f, the transition function of UTM, $f : A \times Q \rightarrow A \times Q \times C$, where $C = \{UP, DOWN, -\}$ is the set of commands given by the automaton to the U/D Counter,
- $\# \in A$ is a special symbol delimiting the active space in RAM.

Therefore, a TM is a three part system: the finite automaton (for control), the infinite automaton (for addressing the RAM), and the infinite RAM.

4.2 Chaitin's Register Machine

G. J. Chaitin ([Chaitin '87, '94]) defines the RM optimizing the UTM⁴. The goal of this approach is to build a Lisp oriented machine with a better solution for list inserting and deleting.

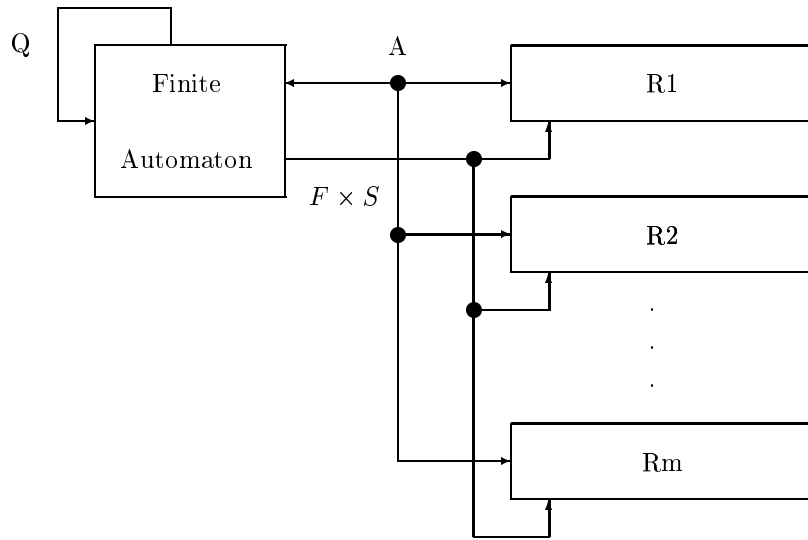


Fig. 5. Registers Machine (RM)

In Fig. 5 the RM has a finite automaton (as interpreter for ToyLisp programs) and a finite number of infinite left/right shift registers used as stacks (initially, in one register we have a Lisp object to be evaluated and the final result will be found in any register).

Definition 4. A RM (see Fig. 5) is a 5-tuple:

$$RM = (A, Q, F, R, g)$$

where:

- A , the finite alphabet (for registers),
- Q , the finite set of states (of the automaton),
- F , the finite set of functions applied to the content of the registers,
 $F = \{READ, WRITE, PUSH, POP\}$,
- R , the finite set of registers,
- g , the transition function of RM, $g : Q \times R \times A \rightarrow Q \times R \times A \times F$.

It is obvious that a RM with minimum two registers is universal.

⁴ to construct his paradoxal Big Omega.

4.3 Connex Memory Machine

A new universal model of computation oriented towards list/tree processing, satisfying all requirements announced in the second section of this paper (fast *access* in any point, easy *insert/delete* in the accessed point, efficient *delimiting* of a substring) is briefly described (for more technical details see [Stefan '85, '86, '94]).

CMM (Fig. 6) has two main parts:

- a finite automaton
- an infinite CM that stores strings of symbols

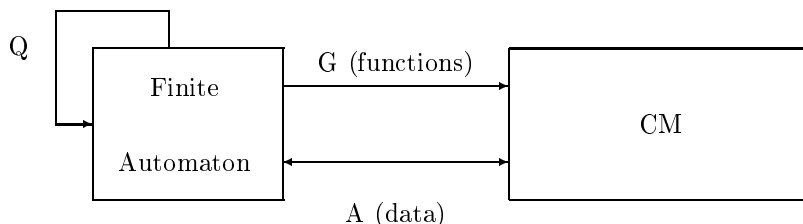


Fig. 6 Connex Memory Machine (CMM)

The differences between CMM and the previous UM models are:

- CMM has only one register which stores any number of strings without access penalties;
- instead of a serial string access, CMM allows a “random” access using associative mechanisms, so the access time is in $O(1)$.

Definition 5. A CMM (see Fig. 6) is a 4-tuple:

$$CMM = (A, Q, G, h)$$

where:

- A , the finite alphabet (for the CM),
- Q , the finite set of states (of the automaton),
- G , is the finite set of CM's functions (see Definition 1 and Definition 2),
- h , is the transition function of CMM, $h : Q \times A \rightarrow Q \times A \times G$.

4.4 Time Performances

The main differences between these three models is the execution time for the basic operations (see Section 2) in string processing: the time for finding (accessing) a point in a string, $T_F(n)$, the time for insert/delete operations, $T_{I/D}(n)$, the time for delimiting substrings of m length, $T_L(m)$.

For the three previous models we have:

- UTM: $T_F(n) \in O(n)$, $T_{I/D}(n) \in O(n)$, $T_L(m) \in O(m)$

- RM: $T_F(n) \in O(n)$, $T_{I/D}(n) \in O(1)$, $T_L(m) \in O(m)$
- CMM: $T_F(n) \in O(1)$ in one cycle, $T_{I/D}(n) \in O(1)$ in one cycle, $T_L(m) \in O(1)$

In all situations the CMM model has a better performance; even more, for $T_F(n)$ and $T_{I/D}(n)$ the execution time is in one cycle [Stefan '86, '94].

5 The ToyLisp Interpreter

We start from the Pure Lisp Model proposed by G. J. Chaitin [Chaitin '87], in which:

- atoms are monosymbolic;
- there are ten primitive functions: ATOM, EQUAL, CAR, CDR, CONS, OUTPUT, QUOTE, IF-THEN-ELSE, EVAL, SAFE-EVAL;
- LAMBDA expressions have the form $(\&vb)$ where v is the list of variables and b is the body;
- for defining variables we use $(\&xe)$ where x is the variable and e is an S-expression with value v ; (xv) is concatenated with the old environment;
- for defining functions we use $(\&(fxyz)d)$ where $fxyz$ is one or more atoms and d is an S-expression; $(f(\&(xyz)d))$ is concatenated with the old environment;
- if an S-expression is not of the form $(\& . . .)$ then it is evaluated in the current environment.

5.1 The Pure Lisp Coprocessor

In order to evaluate ToyLisp programs we conceived a CMM as a Pure Lisp Coprocessor (PLC). The structure of PLC is shown in Fig. 7, where:

- I , is the interface on the host computer bus,
- CA , is the control automaton being able to execute subroutines,
- R , is a register which can store an atom,
- UDC , is an up-down counter used as system symbol generator,
- CM , is the connex memory.

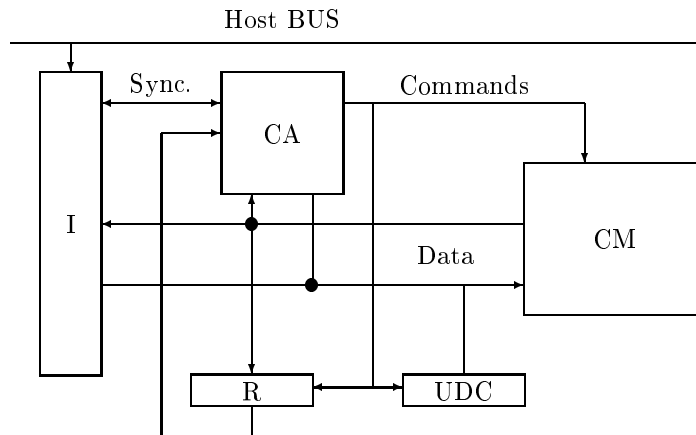


Fig. 7. Pure Lisp Coprocessor

The PLC executes an unending cycle ($print(eval(read))$). The content of the CM is organized as follows:

$@environment\ \$S - expression\ \%temporary\ environment$

and is:

- $@environment\ \% //after\ PRINT//$
- $@environment\ \$S - expression\ to\ be\ evaluated\ \% //after\ READ//$
- $@environment\ \$evaluated\ S - expression\ \%temporary\ environment //after\ EVAL//$

The content of CM is equivalent with the content of three “unbounded” registers that store the environment, the evaluated S-expression and the temporary environment.

5.2 The Interpreter

We are using a *string reduction* mechanism, as it offers a smaller *complexity* of description of the evaluation process. We shall exemplify by describing the CAR function. For more details about the entire interpreter see [Mîțu '96].

```

; (CAR)
; the marker is on + (the CAR sign)
; the substring ...x{+!" s = expr" becomes ...x!" CARs = expr"
; x is marked or the first symbol of the non-evaluated argument is marked
; (setq cm '(z { + ! { { a b } c } } d ) (2) )
; (&car) → ((z ! { a b } d ) (0) )

```

```

(defun &car ()
  (readup)
  (cond((eq(read_) '!) (readup)
        (cond((eq(read_) '{) (&delete) (endsex)
              (insert '{) (readdown) (clrsex) (readup) (backsex))

```

```

    )
    (clrbr) (&delete) (readdown))
))

; (ENDSEX)
; the first symbol of an S-expression is marked and
; the marker will be moved at the beginning of the next symbol
; the pointer is on the first position of m
; if the marker is on a parentheses it is moved after the next paranthesis
; if the marker is an atom it is moved on the next atom
; uses special symbols $ and %
; (setq cm '({ 1 2 { 4 { 6 7 } 9 } }) (0))
; (endsex) → (( { 1 2 { 4 { 6 7 } 9 } }) (11))

(defun endsex ()
  (cond((neq(read_) '{}) (readup))
        (t(insert '$)(insert '})(readup)
           (while(neq(topstack) '})(cond((eq(read_) '{}) (push))
                                         ((eq(read_) '})(pop)))
            (readup)))
        (delstack))
))

; (CLRSEX)
; deletes the S-expression with the marked beginning
; returns cm modified

(defun clrsex ()
  (if(eq '{(read_))
      (progn
        (insert '*)(endsex)(insert '*)(find '*)(readdown)(&delete)
        (while(eq(read_) '*)(&delete))
        (&delete)
        )(&delete)
      )
  ))

; (BACKSEX)
; the first marker is on a right par }
; changes the marker to the corresponding {
; (setq cm '({ a b s d c } f) (7) )
; (backsex) → (({ a b s d c } f) (0))

(defun backsex ()
  (readdown)
  (if(eq(read_) '}')
      (progn
        (readup)(insert '$)(insert '})(readdown)(readdown)(readdown)
        (while(neq(topstack) '})(
          (readdown)
        )
      )
  ))

```

```

        (cond((eq(read_) '})(push))
              ((eq(read_) '{}(pop)))
        )
      (delstack)
    )))

; (CLRBR)
; delete pointed bracket and its corresponding bracket, returns cm modified
; special symbol *
(defun clrbr ()
  (insert '*)(endsex)(readdown)(&delete)(find '*)(readdown)(&delete)
  (&delete))

; (TOPSTACK)
(defun topstack() ;returns the top of the stack, modifies cm
  (let (v)
    (insert '%)(find '$)(setq v(read_))(find '%)(readdown)(&delete)
    v))

; (PUSH) ; pushes the symbol } in the stack after $
(defun push ()
  (insert '%)(find '$)(insert '})(find '%)(readdown)(&delete))

; (POP)
(defun pop () ;pops the symbol from the top of the stack
  (insert '%)(find '$)(&delete)(find '%)(readdown)
  (&delete))

; (DELSTACK)
(defun delstack () ;deletes the stack
  (insert '%)(find '$)(readdown)(&delete)(find '%)(readdown)
  (&delete))

```

5.3 Conclusions

The current approach in Lisp implementation has imposed CAR and CDR as basic functions. Our different way of representing and processing the list in CM, as a *connex* string, may emphasize other basic functions such as: APPEND, MEMBER, LISTATOMS, INTERSECTION, UNION, DELETE, MATCH.

Future work will be focused on optimizing the execution *time* and the *size* of memory, using graph reduction mechanisms. One of the next steps is to test Lisp benchmarks on the simulated PLC in order to compare our approach with other models or frequently used computer architectures.

References

- [Calude '94] Calude, C. : *Information and Randomness*, Springer-Verlag, Berlin, 1994.
- [Chaitin '87] Chaitin, G. J. : *Algorithmic Information Theory*, Cambridge Univ. Press, 1987.
- [Chaitin '94] Chaitin, G. J. : *The Limits of Mathematics IV*, IBM Research Report RC 19671, e-print chaodyn/9407009, July 1994.
- [Hascsi '95] Hascsi, Z., Ștefan, G. : "The Connex Content Addressable Memory (C2AM)", in *Proceedings of 21st European Solid State Circuits*, Lille, France, Sept. 1995, 422-425.
- [Mîțu '96] Mîțu, B., Corina Mîțu : *ToyLisp Interpreter on a Connex Memory Machine*, in C. Calude (ed.). *The Finite, the Unbounded and the Infinite, Proceedings of the Summer School "Chaitin Complexity and Applications"*, Mangalia, Romania, 27 June – 6 July, 1995.
- [Ștefan '85] Ștefan, G., Bistriceanu, V., Păun, A. : "Towards a Natural Mode of Lisp Implementation", in *Systems for Artificial Intelligence*, Romanian Academy Publishing House, Bucharest, 1991, 218-224. (in Romanian)
- [Ștefan '86] Ștefan : "Connex Memory" in *Proceedings of National Conference on Electronics, Telecommunications, Automatics and Computers, Bucharest, 1986* Vol. 2, IPB, București, 1986, 79 - 81. (in Romanian)
- [Ștefan '91] Ștefan, G., Drăghici, F. : "Memory Management Unit - a New Principle for LRU Implementation" in *Proceedings of 6th Mediterranean Electrotechnical Conference*, Ljubljana, Yugoslavia, May 1991, 281-284.
- [Ștefan '94] Ștefan, G.: "The Connex Memory. A Physical Support for Tree / List Processing", *Technical Report*, Center for New Electronic Architecture of the Romanian Academy, February 1994.
- [Ștefan '94a] Ștefan, G., Hascsi, Z.: "The Internal Structure of the Connex Memory", *Technical Report*, Center for New Electronic Architecture of the Romanian Academy, April 1994.
- [Ștefan '95] Ștefan, Mihaela Malita : "The Eco-Chip: A Physical Support for Artificial Life Systems", in *Artificial Life. Grammatical Models*, ed. by Gh. Păun, Black Sea University Press, Bucharest, 1995, 260-275.

A The Connex Memory. First Version: CM1

```

; The First Version of the Connex Memory
; Its Functions are Described in LISP
; Representation: the content of memory is a list  $cm = (s m)$ 
; Where:  $s$  is a list containing the symbols on which we work
;  $m$  is the list of numbers representing the marked position in  $s$ 
; Ex:  $cm = ((a b c a d)(1 4))$  means  $b$  and  $d$  are marked
; the rest are non-marked
; (setq cm '($ nil) )
;  $cm$  is a global variable

; (RST  $p$ )
; all the symbols in  $s$  from  $cm = (s m)$  are substituted with symbol  $p$ 
; all markers are deleted,  $m = ()$ , returns  $cm$ 
; (SETQ CM (QUOTE ((A B C D E) (2 4))))
; (RST (QUOTE P)) → ((P P P P P) NIL)

(defun RST (p) ;  $cm = (sm)$  returns  $cm$ 
(labels((make(p k)
          (if(null k)nil(cons p(make p(cdr k))))))
))
(setq cm(list(make p(car cm)) '())))

; (READ_)
; returns the first marked symbol and  $cm$  is unchanged
; (SETQ CM (QUOTE ((A B C D) (2))))
; (READ_) → C
; CM → ((A B C D) (2))
(defun read_ () (first-marked) )

(defun first-marked () ; $cm = (s m)$  returns first pointed symbol
(let ((n (caadr cm)) (s (car cm)))
  (if (null n) nil (nth n s) ))

; ( $n$ th $nL$ ) returns the  $n$ -th element from  $L$  seen as a vector

; (READUP)
; returns the first marked symbol and modifies  $cm$ 
; moving the marker one position right
; (SETQ CM (QUOTE ((A B C D) (1))))
; (READUP) → B
; CM → ((A B C D) (2))

(defun readup () ;  $cm = (s m)$  returns  $rez$  and modifies  $cm$ 
(let*((s(car cm))(m(cadr cm))(n(car m))(k(cadr m))
(rez(first-marked)))
(cond ((null n)rez)

```

```

      ((and k(= k(1+n)))(setq cm(list s(cdr m))) rez)
      ((>=(1+n)(length s))(setq cm(list s nil))rez)
      (t(setq cm(list s(cons(1+n)(cdr m))))rez)
    )))

```

```

; (READDOWN)
; returns the first marked symbol and modifies cm with
; the first marker moved one position left
; (SETQ CM (QUOTE ((A B C) (1 2))))
; (READDOWN) → B
; CM → ((A B C) (0 2))

```

```

(defun readdown () ; cm = (s m) returns rez
; and modifies the first marker
(let*((s(car cm))(m(cadr cm))(n(car m))(k(cadr m))
(rez(first-marked)))
(cond ((null n)rez)
      ((= n 0)(setq cm(list s(cdr m)))rez)
      ((and k(=n(1+(length s))))(setq cm(list s(cdr m)))rez)
      (t(setq cm(list s(cons(1-n)(cdr m))))rez)
    )))

```

```

; (DELETE)
; returns the first marked symbol and deletes it from cm
; (SETQ CM (QUOTE ((A B C D E F) (1 4))))
; (&DELETE) → B
; CM → ((A C D E F) (1 3))

```

```

(defun &delete () ;cm = (s m) returns first marked symbol
; and modifies cm
(let*((s(car cm))(m(cadr cm))
      (rest(cdr m))(n(car m))(k(cadr m))(rez(first-marked)))
(cond ((null s)(setq cm(list nil nil))rez)
      ((null n)rez)
      ((= n(1+(length s)))(setq cm(list(take n s)(1-n)))rez)
      ((null rest)(setq cm(list(take n s)m))rez)
      ((= n(1-k))(setq cm(list(take n s)(mapcar '1- rest)))rez)
      (t(setq cm(list(take n s)(cons n(mapcar '1-rest))))rez)
    )))

```

```

(defun take(n s) ; takes the n-th element from a list s
(cond ((null s)nil)
      ((= n 0)(cdr s))
      (t(cons(car s)(take(1- n)(cdr s))))
))

```

```

; (INSERT p)

```



```
      ((equal p(nth(car m)s)) (mark p s(cdr m)
                                (cons(1+(car m))r)))
      (t(mark p s(cdr m)r))
    )))
  (setq cm(list s(mark p s m nil)))
  )))
```