The APS Framework For Incremental Learning of Software Agents

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Abstract: Adaptive behavior and learning are required of software agents in many application domains. At the same time agents are often supposed to be resource-bounded systems, which do not consume much CPU time, memory or disk space. In attempt to satisfy both requirements, we propose a novel framework, called APS (standing for Analysis of Past States), which provides agent with learning capabilities with respect to saving system resources. The new solution is based on incremental association rule mining and maintenance. The APS process runs periodically in a cycle, in which phases of agent’s normal performance intertwine with learning phases. During the former ones an agent stores observations in a history. After a learning phase has been triggered, the history facts are analyzed to yield new association rules, which are added to the knowledge base by the maintenance algorithm. Then the old observations are removed from the history, so that in the next learning runs only recent facts are processed in search of new association rules. Keeping the history small can save both processing time and disk space as compared to batch learning approaches.

Key Words: statistical learning, incremental methods, software agents, web browsing assistant

1 Introduction

Adaptivity and learning plays an important role in agent-related research. Since Patti Maes defined the notion of adaptive agents [Maes, 1994], numerous approaches have been developed both for learning of a single agent (Single Agent Learning, SAL) and multi-agent learning (MAL) [Sen and Weiss, 1999]. In many of these works general machine learning methods were adapted to work within agent architectures, e.g.: model-based learning [Maes, 1994, Yao et al. 2002] or reinforcement learning [Ribeiro, 2002]. There are also solutions, where the learning process is an integral part of an agent architecture, such as chunking in Soar [Laird et al. 1987, Newell, 1990].

We propose a new, general framework called APS (standing for Analysis of Past States) for incremental, statistical learning of an agent. It uses data mining algorithms in order to discover association rules in a large set of observations, which are collected by an agent while interacting with an information-rich environment. The APS method first of all is meant to be used within a learning
agent, which operates in a cycle with interlaced phases of performance and being idle. During the former phase the agent works on current tasks: it conducts reasoning, performs actions and perceives information from the outside world. At the same time agent stores in its history some of observed data (e.g. results of performing an action in a given situation). As the observed facts are often too numerous to be efficiently processed on-line (during the performance phase), they are just accumulated as experience for further analysis and learning. A good opportunity for processing the history observations occurs during a stand-by phase, when the agent is not charged with any current task, consequently not utilizing much system resources. Then the agent can switch to learning - analyzing the history facts, discovering new rules and adding them to the rule base with appropriate maintenance of previously existing knowledge.

Consider the following example of a personal web browsing recommender agent, which helps a user choose relevant pages, using a model of preferences, based on accumulated experience. The agent is a silent background process, running at a PC, observing WWW browsing activity and being able to log events, which indicate user’s interest (such as bookmarking, saving or printing a web page). Moreover, the agent provides a simple interface for explicit evaluation of viewed pages (e.g. relevant or irrelevant), if the user wishes so. Every time a user responds to a viewed page in one of the above ways, the agent adds a new fact into the history, with page information (index terms which are frequent in the text, query context etc.) and user’s response (bookmarked, saved, printed, relevant etc.). Depending on browsing activity, the agent can store even hundreds or thousands of such observations weekly. When the history contains a sufficient, representative number of facts\(^1\) and system resources are not loaded heavily, the agent analyses the history, generalizing accumulated knowledge into association rules (e.g. architecture \& development \& schema \(\Rightarrow\) relevant \& stored yes), which can be used later for recommending potentially relevant pages to the user. After the rule mining has been completed, the history is cleared of all the processed facts and newly discovered rules are added to the existing ones using such a maintenance procedure, that the resulting rule base reflects not only the recent analysis, but learning in a longer period. Then the agent can return to normal performance phase, working on tasks and storing new observations for further learning runs. As the history is regularly emptied, its size is kept relatively small, which not only saves disk space, but also CPU time used for learning as compared to batch processing of all the facts stored during the agent’s life-time. Moreover, proper maintenance of the rule base makes it contain stable and statistically reliable rules as if they were discovered in the whole observation history, stored during agent’s life.

\(^1\) Setting a threshold of representative history size is up to a system designer or administrator.
The remainder of the paper is as follows. In section 2 we present a high-level view of the APS learning procedure, while in section 3 we introduce the formal model of knowledge structures and specification of data processing algorithms. In section 4 we show how APS works on an example of a web browsing assistant. The next section contains the plan of experimental evaluation, test data description and discussion of the results. In section 6 the proposed method is compared to related research. Finally, we conclude the contributed work and outline directions of its further development.

2 APS Learning cycle

The key idea of the APS method is to incorporate a general data mining process [Mannila, 1997] into an agent architecture, in order to achieve a rule-based, statistical learning technique. It is based on the procedure, running in a cycle and interacting with the agent’s knowledge base, which consists of four functional modules (see Figure 1). The history \( KB_H \) is a log of collected observations, potentially very numerous. The rule base \( KB_R \) stores rules produced from history facts as their generalization, ready for use in reasoning and decision making. The temporal knowledge module \( KB_T \) is a kind of short term memory, which contains operational data necessary within a single learning run, whereas the general knowledge \( KB_G \) is a long-term memory with information needed across many learning runs. The beneath APS Learning procedure shows the details of the learning process and its interaction with knowledge base modules (input and output data flow).

The key steps of data processing are performed by the algorithms: FSEL, HTRANS, HFILL, ENV, ARM and RMAIN, which are original contribution of this work. The whole loop reflects agent’s life cycle with repeatable performance phases (steps 2-3) and learning phases (steps 4-13). While being in the performance phase an agent works towards its objectives, saving in the history \( KB_H \) selected information about its interaction with the outer world. The designer needs to decide what kind of event is to be captured as a new fact event and what kind of information is to be stored. In the previous web browsing scenario such an event can be bookmarking, saving, printing or evaluating a web page by a user, while the registered information could be frequent index terms describing the page, query context and user’s response. Every new fact put into the history is assigned a unique identifier and timestamp of the very moment of observation. When the number of facts in the history is sufficient (due to some threshold set by a designer) and the agent has no current tasks to perform, the analyze facts event is raised and the APS procedure enters the learning phase (steps 4-13). First, the agent retrieves parameter values from previous learning runs, stored in the \( KB_G \) general knowledge module (step 5). They are necessary for providing continuous processing of incremental data portions. In the next step the
Figure 1: The APS learning cycle in interaction with knowledge base modules.

Procedure 1 APS Learning

**Input:** $KB_G, KB_T, KB_H, KB_R$

**Output:** updated $KB_G, KB_T, KB_H, KB_R$

1: while not Event_Close_Agent_Process do
2:    if Event_New_Fact_Agent_Process then
3:        Store_Fact(input $KB_H$, output $KB_H$)
4:    else if Event_Analyse_Facts then
5:        Get_Parameters (input $KB_G$, output $KB_T$)
6:        Select_Facts (input $KB_H$, $KB_T$, output $KB_H$, $KB_T$)
7:        Transform_History_Schema (input $KB_H$, output $KB_H$, $KB_T$)
8:        Fill_New_Schema (input $KB_H$, output $KB_H$)
9:        Remove_N_Values (input $KB_H$, $KB_T$), output $KB_H$, $KB_T$)
10:       Mine_Rules (input $KB_H$, $KB_T$, output $KB_T$)
11:      Update_Rule_Base (input $KB_R$, $KB_T$, $KB_G$, output $KB_R$, $KB_G$)
12:     Delete_Facts (input $KB_H$, $KB_T$, output $KB_H$)
13:     end if
14: end while
The FSEL algorithm chooses a set of recent history facts for rule discovery in the current run. By default all the observations in $KB_H$ are retrieved. Afterwards, the selected facts are transformed to the acceptable input format for a data mining algorithm - namely transactions with binary attributes. First, a new history schema is created, using the HTRANS algorithm (step 7) and then it is filled with transformed facts by the HFILL algorithm (step 8). During further preprocessing transactions with unknown values are replaced by all the possible facts, using the ENV algorithm (step 9). The prepared history facts are then analyzed by an association rule mining algorithm (e.g. Apriori [Agrawal et al. 1994]), incorporated into the ARM algorithm (step 10), which plays a role of an interface between a mining algorithm and the APS procedure. After a set of new association rules $R$ has been discovered, it is combined with the former rule base in $KB_R$ (step 11) so that the resulting rule set reflected all the facts analyzed so far (i.e. in the current and previous learning runs). The necessary rule maintenance is done by the RMAIN algorithm, which is truly essential for the whole method. Then, the recently processed history observations are disposed (step 12), updated parameter values needed for further learning runs are saved in the general knowledge $KB_G$, while the temporal knowledge module $KB_T$ is cleared of all the information concerning the recent run and the agent switches back to the performance phase.

The presented approach of periodic clearing the history can be classified as \textit{learning with imperfect recall} [Dudek et al. 2005, Fagin et al. 1995] and \textit{partial memory learning} [Maloof and Michalski, 2004]. Nevertheless, although the agent forgets elementary past events, it keeps and maintains rules, which are general conclusions about observations, potentially useful for reasoning.

3 Formal model

After the overview of the APS method given in the previous section, we present formal specification of knowledge base structures and data processing algorithms. Some preliminary elements of the APS model were introduced briefly in the previous work [Dudek et al. 2005], while a general presentation of the APS method without detailed formalism was introduced in [Dudek, 2007].

3.1 Knowledge base structure

Below we formally define data structures and some auxiliary elements, which are used in the APS learning cycle. The presented model is partly based on the relational database notation by Pankowski [Pankowski, 1992]. It also refers to models of transaction databases and association rules provided in [Agrawal et al. 1993,
Agrawal et al. 1994]. However, our model is significantly richer, covering non-binary and multi-valued attributes, extended rule representation, time depreciation functions and original APS agent’s knowledge modules.

**Definition 1 Fact.** Let \( S_H = \{K, T, U\} \) be called a schema, where the symbol \( K \) is a key, the symbol \( T \) is time, and \( U \) is a finite set of attributes \( U = \{A^S_1, \ldots, A^S_n, A^M_1, \ldots, A^M_k\} \). The elements \( A^S_i \in U \), for \( i = 1, \ldots, n \) (\( n \in \mathbb{N} \)) are called single-valued attributes, and \( A^M_j \in U \), for \( j = 1, \ldots, k \) (\( k \in \mathbb{N} \)) are called multi-valued attributes. Let \( K \) and \( T \) be assigned respectively a set \( D_K \subseteq \mathbb{N} \) called the key domain and a countable set of time points \( D_T \), which is ordered by a strong linear order relation \(<\). Let each single-valued attribute \( A^S_i \), for \( i = 1, \ldots, n \) be assigned a domain, which is a finite set of values \( D^S_i \). Let each multi-valued attributed \( A^M_j \), for \( j = 1, \ldots, k \), be assigned a domain, which is a set \( D^M_j = 2^U \) of all possible subsets of a finite set \( V_j \). A fact of a schema \( S_H = \{K, T, U\} \) is defined to be any function \( s \), such that: \( s: \{K, T, U\} \to D_K \cup D_T \cup \bigcup \{D^S_i : A^S_i \in U, i = 1, \ldots, n\} \cup \bigcup \{D^M_j : A^M_j \in U, j = 1, \ldots, k\} \).

Multi-valued attributes are very useful for description of real-life objects. For instance a web page can be characterized by a multi-valued attribute term, which is assigned a collection of values – terms describing this document. We denote a fact \( s \) of a schema \( S_H = \{K, T, U\} \) as a set of attribute-value pairs \( s = \{(K, k), (T, t), (A^S_1, a^S_1), \ldots, (A^S_n, a^S_n), (A^M_1, a^M_1), \ldots, (A^M_k, a^M_k)\} \), where \( A^S_i, A^M_j \in U \), for \( i = 1, \ldots, n \) and \( j = 1, \ldots, k \).

Values of the key \( K \), time \( T \), a single-valued attribute \( A^S_i \) and a multi-valued attribute \( A^M_j \) in a fact \( s \) are denoted as: \( K(s) = k \), \( T(s) = t \), \( A^S_i(s) = a^S_i \), and \( A^M_j(s) = a^M_j \), respectively. We denote an unknown value of an attribute (single- or multi-valued) by a symbol \( N \). A set of all single-valued attributes \( A^S_i \in U \) for \( i = 1, \ldots, n \) in a schema \( S_H = \{K, T, U\} \) is denoted by \( S^S_H \), while similar set of all multi-valued attributes \( A^M_j \in U \) for \( j = 1, \ldots, k \) is denoted by \( S^M_H \). The following properties are satisfied: \( S^S_H \subseteq S_H \setminus \{K, T\} \), \( S^M_H \subseteq S_H \setminus \{K, T\} \), and \( S^S_H \cap S^M_H = \emptyset \). A set of all the facts of a schema \( S_H \) is denoted by a symbol \( FACT(S_H) \). We allow solely discrete attribute domains, which potentially implies necessity of discretization for continuous domains (e.g. real numbers). However, dealing with problem is strongly domain-dependent and goes beyond the scope of this paper.

**Definition 2 History.** Let a schema \( S_H = \{K, T, U\} \) be given. A history \( KB_H \) of a schema \( S_H \) is any subset of the set of all facts of the schema \( S_H \). Formally: \( KB_H \subseteq FACT(S_H) \).

We denote: the \( k \)-th time point belonging to the set \( D_T \) by \( t_k \), the time point of the first fact in the history by \( t_0 \), the time point referring to the presence by \( t_{\text{now}} \), and the time interval from the moment \( t_i \) until \( t_j \), where \( t_i \leq t_j \), by \( [t_i; t_j] \). For each fact \( s \in KB_H \) the following dependency is satisfied: \( t_0 \leq T(s) \leq t_{\text{now}} \).
**Definition 3 Fact portion.** Let a history $KB_H$ of a schema $S_H = \{K,T,U\}$ be given. A fact portion of the history $KB_H$ for the time interval $[t_1:t_2]$, where $t_1, t_2 \in D_T \land t_1 \leq t_2$, is the set: $KB_H(t_1,t_2) = \{s \in KB_H : t_1 \leq T(s) \leq t_2\}$.

**Definition 4 Proper domain of a single-valued attribute.** Let a history $KB_H$ of a schema $S_H = \{K,T,U\}$ be given. A proper domain of a single-valued attribute $A_i^S \in S_H^S$ in the history $KB_H$ for the time interval $[t_1:t_2]$, where $t_1, t_2 \in D_T \land t_1 \leq t_2$, is a set: $D^W_i(KB_H(t_1,t_2)) = \{A_i^S(s) \neq N : s \in KB_H \land (t_1 \leq T(s) \leq t_2)\}$.

**Definition 5 Proper domain of a multi-valued attribute.** Let a history $KB_H$ of a schema $S_H = \{K,T,U\}$ be given. A proper domain of a multi-valued attribute $A_i^M \in S_H^M$ in the history $KB_H$ for the time interval $[t_1:t_2]$, where $t_1, t_2 \in D_T \land t_1 \leq t_2$, is a set: $D^W_i(KB_H(t_1,t_2)) = \bigcup\{A_i^M(s) \neq \emptyset : s \in KB_H \land (t_1 \leq T(s) \leq t_2)\} \setminus \{N\}$.

The proper domain of an attribute is a set of all its values (except for the unknown value $N$), which are actually present in a given subset of history facts. Narrowing attribute values to their proper domains (as opposed to all the possible values) allows to speed up transformation of the history to the format with binary attributes and $N$-values $\{0,1,N\}$.

**Definition 6 Rule.** Let a set $U' = \{A_1,A_2,\ldots,A_m\}$ of binary attributes be given. Each attribute $A_i$ where $i = 1,2,\ldots,m$ is assigned a set of values $D_b = \{0,1,N\}$. Let a countable set of time points $D_T$ be given, ordered by the relation $<$ of strong linear order. A rule $r$ is defined as a tuple: $r = (X,Y,\text{sup},\text{con},b,t_m) \in 2^{U'} \times 2^{U'} \times [0;1] \times [0;1] \times N \times D_T$, where: $X$ is called antecedent, $Y$ – consequent, $\text{sup}$ – support, $\text{con}$ – confidence, $b$ – base number, $t_m$ – mean time of the rule.

The above rule representation extends a classical association rule definition, used in many works (such as the one proposed in [Agrawal et al. 1993, Agrawal et al. 1994]). The novel elements needed for the APS incremental learning process are: (i) the base number $b$ – the number of history facts, based on which the rule $r$ was discovered, (ii) mean time $t_m$ of these facts.

**Definition 7 Syntactical equity of rules.** Two rules $r_1 = (X_1,Y_1,\text{sup}_1,\text{con}_1, b_1,t_{m1})$ and $r_2 = (X_2,Y_2,\text{sup}_2,\text{con}_2,b_2,t_{m2})$, where $r_1, r_2 \in 2^{U'} \times 2^{U'} \times [0;1] \times [0;1] \times N \times D_T$, are said to be syntactically equal, denoted by $r_1 \equiv r_2$, iff $X_1 \equiv X_2 \land Y_1 \equiv Y_2$.

**Definition 8 Rule base.** Let a set $U' = \{A_1,A_2,\ldots,A_m\}$ of binary attributes be given. Each attribute $A_i$ for $i = 1,2,\ldots,m$ is assigned a set of values $D_b = \{0,1,N\}$. Let a countable set of time points $D_T$ be given. A rule base $KB_R$ is the following set:
Definition 9 Vector of current run parameters. Let \( U \) and \( D_T \) be defined as before. A vector of current run parameters is a tuple:

\[
v_c = (id_c, X_c, Y_c, b_{\text{max}}, b_c, \eta_c, \sigma_c, \gamma_c, \hat{\gamma}_c, m_x, m_y, t_{\text{rc}}, t_{\text{mc}}, t_{\text{sc}}, t_{\text{ec}}, k_{\text{ec}}) \in \mathbb{N} \times 2^U \times 2^U \times \mathbb{N} \times \mathbb{N} \times [0; 1] \times [0; 1] \times [0; 1] \times 2^T \times 2^T \times 2^T \times 2^T \times \mathbb{N}
\]

where \( \hat{\sigma}_c \in [0; \sigma_c] \land \hat{\gamma}_c \in [0; \gamma_c] \land t_{\text{mc}} \leq t_{\text{sc}} \leq t_{\text{ec}} \).

The symbol \( id_c \) is a unique run identifier, \( X_c \) and \( Y_c \) – a set of attributes, which are allowed in the rule antecedent and consequent, respectively; \( b_{\text{max}} \) – the maximal number of facts, which can be analyzed during the current run; \( b_c \) – the number of facts actually analyzed in the current run; \( \eta_c \) – the maximal number of allowed \( N \)-values in a single fact; \( \sigma_c \) and \( \gamma_c \) – thresholds of minimum rule support and confidence, respectively; \( \hat{\sigma}_c \) and \( \hat{\gamma}_c \) – expected support and confidence of rejected rules; \( m_x \) and \( m_y \) – the maximal number of attributes in the rule antecedent and consequent, respectively; \( t_{\text{rc}} \) – time of starting the current run; \( t_{\text{mc}}, t_{\text{sc}}, t_{\text{ec}} \) – the mean, the earliest and the latest time of facts analyzed in the current run; \( k_{\text{ec}} \) – the key of the last analyzed fact. In the APS framework the \( v_c \) vector of current run parameters belongs to the temporal knowledge module \( KB_T \), i.e. \( v_c \in KB_T \). We do not provide a formal definition of \( KB_T \), as its structure depends on an application domain.

Definition 10 Time depreciation function. The time depreciation function is any function \( f_T : [0; +\infty) \to [0; 1] \), such that: (i) \( f_T(0) = 1 \) and (ii) \( \forall x_1, x_2 \in [0; +\infty). x_1 < x_2 \Rightarrow f_T(x_1) \geq f_T(x_2) \).

We denote the family of all \( f_T \) functions by \( \mathcal{F} \). The argument of the \( f_T \) function is time, which has passed since a given past moment \( t \) until \( t_{\text{now}}, \) i.e. \( (t_{\text{now}} - t) \), for time points \( t, t_{\text{now}} \in D_T \). For the current moment \( t = t_{\text{now}} \) the \( f_T \) function achieves the maximal value 1. The actual formula and parameters of a \( f_T \) function depend on a given application (see Figure 2 for example shapes).

Definition 11 Vector of global parameters. Let \( \mathcal{F} \) and \( D_T \) be defined as before. A vector of global parameters is a tuple:

\[
v_g = (b_g, \sigma_g, \gamma_g, \hat{\gamma}_g, t_{mg}, t_{sg}, t_{eg}, k_{eg}, f_T) \in \mathbb{N} \times [0; 1] \times [0; 1] \times [0; 1] \times 2^T \times 2^T \times 2^T \times \mathbb{N} \times \mathcal{F}, \text{ where: } \hat{\sigma}_g \in [0; \sigma_g] \land \hat{\gamma}_g \in [0; \gamma_g] \land t_{sg} \leq t_{mg} \leq t_{eg}.
\]

The components of the vector concern all the learning runs performed so far: \( b_g \) – the number of facts which were analyzed; \( \sigma_g \) and \( \gamma_g \) – thresholds of minimal support and confidence; \( \hat{\sigma}_g \) and \( \hat{\gamma}_g \) – expected support and confidence of rejected rules; \( t_{mg} \) mean time of all processed facts; \( t_{sg} \) and \( t_{eg} \) – time of the first and the last analyzed fact; \( k_{eg} \) – the key of the last analyzed fact;
Figure 2: Example shapes of the $f_T$ time depreciation function.

$f_T$ – time depreciation function (formula and parameters). The defined vector of global parameters belongs to the general knowledge module (long-term memory), denoted by $KB_G$, together with the history schema, i.e. $v_g \in KB_G \land S_H \in KB_G$.

3.2 Data processing algorithms

In the current subsection we introduce original algorithms for data processing inside the APS cycle\(^1\). We omit two procedures Store_Facts (step 3) and Get_Parameters (step 5), which are domain-dependent, but also quite simple and straightforward. An intuitive example of how the proposed APS algorithms work is presented in Section 4.

3.2.1 Selecting facts for analysis

In the step 6 the APS procedure selects history facts, which are to be processed in the current learning cycle. The task can be described as follows. Given the history $KB_H$ with a schema $S_H = \{K, T, U\}$ and the maximal number of facts to be retrieved $b_{max}$, find a portion of facts $KB_H(t_{sc},t_{ec})$, such that:

$$|KB_H(t_{sc},t_{ec})| \leq b_{max} \text{ and } \forall s \in KB_H(t_{sc},t_{ec}). t_{sc} \leq T(s) \leq t_{ec} \land \neg \exists s' \in KB_H \setminus KB_H(t_{sc},t_{ec}). T(s') < T(s).$$

In other words, at most $b_{max}$ of the earliest facts are to be selected, whose registration time lies within the given interval. The name of the solution algorithm FSEL comes from Fact SELection.

Provided that the history $KB_H$ is managed by a relational database engine (RDBMS), selecting facts is a simple operation, which can be effectively realized by SQL commands such as SELECT TOP N...FROM...ORDER BY, together with aggregation functions: MIN, MAX, AVERAGE. The computational complexity of FSEL is linear: $O(n)$, where $n$ is the number of facts in $KB_H$.

\(^1\) Some elements and preliminary versions of the algorithms were introduced in the previous works [Dudek and Zgrzywa, 2005, Dudek et al. 2005], while their thorough analysis (including computational complexity) was done in [Dudek, 2005].
3.2.2 Transforming the history schema

After history facts are selected, the APS procedure needs to transform them into a form with binary attributes, which would be acceptable for a data mining process. First we need a new attribute schema, which can be further filled with facts. This is done by the Transform_History_Schema procedure (step 7) of the APS cycle. Formally, the problem can be stated as follows. Given the history schema \( S_H = \{K,T,U\} \) and the selected fact portion \( KB_H(t_1, t_2) \), find a new schema \( S^\# = \{K,T,U'\} \), such that \( \forall A_i \in U' \), \( D_i = \{0,1\} \). The only non-binary attributes allowed in the new schema are special attributes: the key \( K \) and the timestamp \( T \), which remain unchanged as compared to the previous history schema. As a solution we propose the following HTRANS (History schema TRANSformation) algorithm. Attributes \( A_i^{(v)} \) of the new \( S^\# \) schema are found based on proper domains of initial attributes \( A_i \) (both single and multi-valued) that is all distinct values (except for \( N \)) which occurred in the processed fact portion. Observe that transforming the history schema in every APS learning run potentially narrows the number of resulting binary attributes, as compared to building a huge, general schema suitable for all runs (thus possibly containing many redundant attributes for a single run). Moreover, in our approach different history attributes can be used during different periods of storing observations. The complexity of the HTRANS algorithm is \( O(k^2 mn) \), where \( n \) is the number of facts in the portion \( KB_H(t_1, t_2) \), \( m \) is the number of attributes in \( U \), and \( k \) is average number of attribute’s distinct values in that portion.
### Algorithm 2 HTRANS: Transforming the history schema

**Input:** history schema $S_H = \{K,T,U\}$, selected fact portion $KB_H(t_{sc}, t_{ec})$

**Output:** the new schema $S^#$

1. $S^# := \emptyset$
2. $S^# := S^# \cup \{K,T\}$
3. for all $A_i \in U$, where $i \in [1; |U|]$ do
4.   find $D^W(KB_H(t_{sc}, t_{ec}))$.
5.   $S^# := S^# \cup \{A_i^{(v)}: A_i \in S_H \land v \in D^W(KB_H(t_{sc}, t_{ec}))\}$.
6. end for
7. return $S^#$

#### 3.2.3 Populating the new schema

We transform on the fly the facts from the initial portion $KB_H(t_{sc}, t_{sc})$ into the new $S^#$ schema, using the following HFILL algorithm (History FILLing). The resulting portion $KB^T_H(t_{sc}, t_{sc})$ consists of the same number of facts as $KB_H(t_{sc}, t_{sc})$. Single-valued attributes are processed through straightforward value comparison (steps 4–12), while for multi-valued ones set membership needs to be tested (steps 13–21). Assume that the portion $KB_H(t_{sc}, t_{sc})$ consists of $n$ facts and the set $U'$ of the schema $S^# = \{K,T,U'\}$ contains $m$ attributes, $n, m \in \mathbb{N}$. Then the HFILL algorithm has computational complexity of $O(mn)$.

#### 3.2.4 Eliminating unknown values

The facts transformed to the schema with binary attributes may be still unacceptable for many association rule mining algorithms as long as they contain unknown values $N$. We propose the ENV algorithm (Elimination of N Values) to deal with this problem. Essentially, the idea is to replace a fact containing one or more $N$ values, with all the possible scenarios without $N$ values. We use here the random worlds approach, treating all the possibilities equally probable [Bacchus et al. 1996]. This solution, even though simplified, decreases complexity of $N$ value removal process and still provides good reliability of reasoning in information rich environments, as shown in [Bacchus et al. 1996]. In order to ensure consistency of generated facts, a complex condition is used in step 4. It guarantees that only one binary attribute $A_i^{(v_j)} \in S^#$ coming from a single-valued attribute $A_i \in S_H^#$ can have value 1, while for multi-valued attributes $A_w \in S_H^M$ there can be more than one derived binary attribute $A_w^{(v_j)} \in S^#$ with value 1. If there are more than $\eta$ unknown values in a fact, it is considered too little informative and deleted without replacement\(^2\). After all $N$ values have

\(^2\) At the same time, reducing the number of facts decreases computational complexity of ENV.
been removed, time parameters $t_{sc}$ and $t_{ec}$ of the $v_c$ vector are adjusted to the new set of facts\footnote{Either the first or the last fact could have been removed, if it contained too many $N$ values.}.

The ENV algorithm has high, non-polynomial complexity of $O(n2^m)$, pro-
vided that \( KB_H^#(t_{sc}; t_{ec}) \) contain \( n \) facts, \( k \) of them have at least one unknown value, and let the maximal number of \( N \) values in a single fact be \( m \), where \( k, m, n \in \mathbb{N} \) and \( k \leq n \). Hence, this algorithm should be used carefully and parameterized with possibly low \( \eta_c \) threshold values.

### 3.2.5 Association rules discovery

After the history facts have been preprocessed, they can be analyzed by the rule mining procedure, using an algorithm chosen by the system developer (e.g. Apriori). The association discovery alone follows classical problem statement presented in other works [Agrawal et al. 1993, Agrawal et al. 1994, Goethals, 2002], but the novel solution is to place a rule mining algorithm inside the ARM algo-
Algorithm 5 ARM: Association rules discovery

Input: preprocessed fact portion $KB^F_H(t_{sc}; t_{ec})$, vector $v_c \in KB_T$, including
constraints $X_c(v_c), Y_c(v_c), \sigma_c(v_c), \gamma_c(v_c), m_x(v_c), m_y(v_c), b_c(v_c), t_{mc}(v_c)$

Output: set of new rules $R$

1: $R := \emptyset$
2: if the rule mining algorithm accepts constraints concerning the rule antecedent $X$ and consequent $Y$ then
3: $R := \text{Rule\_Mining\_Algorithm}(\sigma_c, \gamma_c, X_c, Y_c, m_x, m_y)$
4: else if the rule mining algorithm does not accept constraints concerning $X$ and $Y$ then
5: $R := \{ r \in R: X(r) \subseteq X_c \land Y(r) \subseteq Y_c \land |X(r)| \leq m_x \land |Y(r)| \leq m_y \}$
6: end if
7: if $\neg R \equiv \emptyset$ then
8: for all rules $r_i \in R$, $i \in [1; |R|]$ do
9: $b(r_i) := b_c(v_c)$
10: $t_m(r_i) := t_{mc}(v_c)$
11: end for
12: end if
13: return $R$

Computational complexity of the ARM algorithm is strictly dependent on the encapsulated $\text{Rule\_Mining\_Algorithm}$. Hence, it can be considered beneficial that we do not force any specific algorithm, but allow a developer choose the
best one available. Additional workload of the steps 6 and 9–11 does not seem to be a serious problem, as it gives linear complexity of $O(n)$, where $n$ is the number of rules $r \in R$.

### 3.2.6 Rule base maintenance

Updating the rule base $KB_R$, when old rules are combined with new ones $R$, is truly the crucial phase of the whole APS cycle. This maintenance is to keep the rule base in such a shape, as if all the rules were discovered in a single batch of history facts, accumulated since the very beginning of APS learning, even though actually only a recent portion of observations is processed in every run and analyzed past events are disposed. Formally, given two rule sets $KB_R$ and $R$ found in sets of facts $h_1$ and $h_2$, where $h_1 \cap h_2 \equiv \emptyset \land \forall s_1 \in h_1, \forall s_j \in h_2, T(s_i) < T(s_j)$, the new, combined rule set $KB'_R$ is to be found, such that $KB'_R \cong KB^S_R$, where $KB^S_R$ is a rule set found in $h_1 \cup h_2$.

As a solution to the stated problem we introduce the RMAIN algorithm\(^4\) (*Rule MAINtenance*). Its key idea is to find pairs of rules – one from $KB_R$ and the other one from $R$ – with similar antecedents and consequents, and combine their support, confidence and other parameters, using appropriate proportion formulae (see the RMAIN algorithm). If a given rule does not exist in one of the combined sets, we use estimators of expected support $\hat{\sigma}$ and confidence $\hat{\gamma}$, which substitute corresponding values of a hypothetical, rejected rule (because of too low support or confidence), in order to decrease computation error [Dudek, 2005]. Moreover, we use the time depreciation function $f_T : [0; +\infty) \to [0; 1]$ (see Definition 10 in the section 3.1) in order to promote recent rules and deprecate old ones. Otherwise, in subsequent learning runs the old rules would be more and more resistant to any changes.

In the algorithm three cases of rule comparison are considered: (i) stable rules, which are present both in $R$ and $KB_R$ (steps 2–7); (ii) new rules, which belong to $R$, but are not found in $KB_R$ (steps 2, 8–12); (iii) old rules, which belong solely to $KB_R$ and are not present in $R$ (steps 15–20). In each case rule’s support, confidence, base number and time are updated, using proportion formulae. However, in cases (ii) and (iii) the unknown values of rule parameters are approximated by the estimators. After parameter update, new rules from $R$ can be added to $KB_R$, if only they satisfy minimum support and confidence thresholds. At the same time old rules are withdrawn from $KB_R$, if their updated support or confidence do not meet the threshold requirements. In order to simplify the formulae notation inside the RMAIN algorithm, we use the following abbreviations: $f_{p_j} = f_t(t_{\text{now}} - t_m(p_j))$, $f_{r_i} = f_t(t_{\text{now}} - t_m(r_i))$, $f_{g} = f_t(t_{\text{now}} - t_{mg})$, $f_{c} = f_t(t_{\text{now}} - t_{mc})$.

\(^4\) A preliminary version of the RMAIN algorithm was introduced in the previous work [Dudek and Zgrzywa, 2005].
Algorithm 6 RMAIN: Rule base maintenance

Input: \( KB_R, R \); vectors \( v_c \in KB_T \) and \( v_g \in KB_G \); current system time \( t_{now} \)

Output: updated \( KB_R \) and \( v_g \in KB_G \)

1: update \( v_g \): \( \sigma(v_g) := \frac{\sigma(v_g) b(v_g) + \sigma(v_c) b(v_c)}{b(v_g) + b(v_c)} \), \( \gamma(v_g) := \frac{\gamma(v_g) b(v_g) + \gamma(v_c) b(v_c)}{b(v_g) + b(v_c)} \)

2: for all rules \( r_i \in R, i \in [1; |R|] \) do

3: if \( \exists p_j \in KB_R, p_j \equiv r_i \) then

4: update \( p_j \): \( sup(p_j) := \frac{b(p_j) sup(p_j)_f p_j + b(r_i) sup(r_i)_f r_i}{b(p_j) + b(r_i)} \),

   \( con(p_j) := \frac{con(p_j) con(r_i)_f b(p_j) sup(p_j)_f p_j + b(r_i) sup(r_i)_f r_i}{b(p_j) + b(r_i)} \),

   \( t_m(p_j) := \frac{b(p_j) t_m(p_j)_f p_j + b(r_i) t_m(r_i)_f r_i}{b(p_j) + b(r_i)} \), \( b(p_j) := b(p_j) + b(r_i) \).

5: if after the update \( sup(p_j) < \sigma(v_g) \) or \( con(p_j) < \gamma(v_g) \) then

6: \( KB_R := KB_R \setminus \{p_j\} \)

7: end if

8: else if \( \neg \exists p_j \in KB_R, p_j \equiv r_i \) then

9: update \( r_i \): \( sup(r_i) := \frac{b(v_g) \bar{\sigma}(v_g) + b(r_i) sup(r_i)_f r_i}{b(v_g) + b(r_i)} \),

   \( con(r_i) := \frac{\bar{\gamma}(v_g) con(r_i)_f b(v_g) \bar{\sigma}(v_g) + b(r_i) sup(r_i)_f r_i}{b(v_g) + b(r_i)} \), if \( 0 < \bar{\gamma}(v_g) \leq 1 \),

   \( \bar{\gamma}(v_g) := con(r_i), \) if \( \bar{\gamma}(v_g) = 0 \),

   \( t_m(r_i) := \frac{b(v_g) t_m(r_i)_f r_i + b(r_i) t_m(r_i)_f r_i}{b(v_g) + b(r_i)} \), \( b(r_i) := b(v_g) + b(r_i) \).

10: if after the update \( sup(r_i) \geq \sigma(v_g) \) and \( con(r_i) \geq \gamma(v_g) \) then

11: \( KB_R := KB_R \cup \{r_i\} \)

12: end if

13: end if

14: end for

15: for all rules \( p_j \in KB_R \), such that \( \neg \exists r_i \in R, p_j \equiv r_i \) do

16: update \( p_j \): \( sup(p_j) := \frac{b(p_j) sup(p_j)_f p_j + b(v_g) \bar{\sigma}(v_c) f c}{b(p_j) + b(v_g)} \),

   \( con(p_j) := \frac{con(p_j) \bar{\gamma}(v_g)_f b(p_j) sup(p_j)_f p_j + b(v_g) \bar{\sigma}(v_c) f c}{b(p_j) + b(v_g)} \), if \( 0 < \bar{\gamma}(v_g) \leq 1 \),

   \( \bar{\gamma}(v_g) := con(p_j), \) if \( \bar{\gamma}(v_g) = 0 \),

   \( t_m(p_j) := \frac{b(p_j) t_m(p_j)_f p_j + b(v_g) t_m(v_g)_f v_g}{b(p_j) + b(v_g)} \), \( b(p_j) := b(p_j) + b(v_g) \).

17: if after the update \( sup(p_j) < \sigma(v_g) \) or \( con(p_j) < \gamma(v_g) \) then

18: \( KB_R := KB_R \setminus \{p_j\} \)

19: end if

20: end for

21: update the vector \( v_g \): \( \hat{\sigma}(v_g) := \frac{\hat{\sigma}(v_g) b(v_g) + \bar{\sigma}(v_c) b(v_c)}{b(v_g) + b(v_c)} \),

   \( \bar{\gamma}(v_g) := \frac{\hat{\gamma}(v_g) b(v_g) + \bar{\gamma}(v_c) b(v_c)}{b(v_g) + b(v_c)} \), \( t_m(v_g) := \frac{b(v_g) t_m(v_g)_f v_g + b(v_g) t_m(v_g)_f v_g}{b(v_g) + b(v_c)} \),

22: update the vector \( v_g \): \( b(v_g) := b(v_g) + b(v_g) \)

23: return updated \( KB_R \) and \( v_g \)
The complexity of RMAIN is polynomial \(O(mn)\), where \(n\) is the number of new rules in \(R\) and \(m\) is the number of old rules in \(KB_R\), \(m, n \in \mathbb{N}\). Other properties of the RMAIN algorithm were analyzed in [Dudek, 2005].

4 Example: web browsing assistant

In order to illustrate how the APS learning cycle works, we present the beneath example, referring to the personal web browsing assistant agent scenario (described in the Introduction). The agent history \(KB_H\) is as table containing the following columns (see Figure 3): \(HKey\), \(HTime\), \(Term\), \(Eval\), and \(Stored\), representing: unique key, observation moment, collection of frequent index terms in the page (multivalued column), user’s evaluation (relevant or irrelevant), and information about saving a page (yes or no), respectively. \(N\) values are placed into cells with missing information (e.g. a page stored without any evaluation).

The first step of the APS learning run is the FSEL algorithm, which selects a block of recent observations, stored in the history since the previous processing run. Then these facts are transformed by the HTRANS algorithm from the initial schema: \(S_H = \{HKey, HTime, Term, Eval, Stored\}\) into the schema: \(S^# = \{HKey, HTime, Term^{(architecture)}, Term^{(base)}, ..., Term^{(server)}, Eval^{(relevant)}, Eval^{(irrelevant)}, Stored^{(yes)}, Stored^{(no)}\}\).

All the attributes of the new schema can accept only two values: 1 (positive assertion) and 0 (negative assertion), except for the first two special columns \(HKey\) and \(HTime\), which are left unchanged. In the next step of the APS run, the new \(S^#\) schema is filled with history facts by the HFILL algorithm (see Figure 4). Following the APS cycle, \(N\) values are eliminated using the ENV algorithm. Each row with unknown values is removed and instead new facts are inserted into the history, which reflect all the possible worlds (Figure 4). However, a row containing more \(N\) values than a presumed threshold \(\eta_c\), is just dropped without any replacement (this case is not shown in Figure 4).

The transformed and preprocessed history is now ready for association rule mining, managed by the ARM algorithm. Let’s assume that after analyzing 500 recent \(KB_H\) facts, two new rules were found (the \(R\) set): \(r_1: \text{term}_1, \text{architecture} \wedge \text{base}_1\) and \(r_2: \text{term}_2, \text{architecture} \wedge \text{server}_1\).
The newly discovered rules $r_1$ and $r_2$ need to be added to the $KB_R$ rule base, which has contained two rules since the previous APS learning run (both based on 3000 processed facts): $p_1: \text{term\_architecture} \land \text{term\_schema} \Rightarrow \text{eval\_relevant} \ (sup = 0.12; \ con = 0.73; \ b = 3000; \ t_m = 2008/01/16 10:45)$ and $p_2: \text{term\_copy} \land \text{term\_mechanism} \Rightarrow \text{stored\_yes} \ (sup = 0.21; \ con = 0.69; \ b = 3000; \ t_m = 2008/01/16 10:45)$. It appears that the rules $r_1$ and $p_1$ are syntactically equal (see Definition 7), i.e. they have the same antecedents and consequents and only values of their support and confidence are different. In the $R$ rule set $r_2$ is a new rule, which has been just found in the recent learning run. On the other hand the rule $p_2$ in $KB_R$ has not been discovered lately, so we can expect its support and confidence will be decreased during $KB_R$ update.

In the next stage, both rule sets $R = \{r_1,r_2\}$ and $KB_R = \{p_1,p_2\}$ are combined with each other by the RMAIN rule maintenance algorithm. Three cases are considered while updating $KB_R$: (i) the rules in both sets, which are syntactically equal ($r_1$ and $p_1$ in our example) – steps 2–7 of the algorithm; (ii) the rules, which exist only in $R$ (rule $r_2$) – steps 2, 8–12, and (iii) the rules, which exist only in $KB_R$ and were not discovered during the recent mining run (rule $p_2$) – steps 15–20. For RMAIN calculations we assume the following input parameters (see Definitions 9 and 11). The vector of current run parameters $v_c$: $X_c = \{\text{Term}\}$; $Y_c = \{\text{Eval}, \text{Stored}\}$; $b_{max} = 500; \ b_c = 500; \ \eta_c = 0; \ \sigma_c = 0.06; \ \gamma_c = 0.70; \ \hat{\sigma}_c = 0.03; \ \hat{\gamma}_c = 0.35; \ m_x = 4; \ m_y = 1; \ t_{rc} = t_{now} = 2008/05/21 18:05; \ t_{mc} = 2008/05/17 04:04; \ t_{sc} = 2008/04/19 16:30; \ t_{ec} = 2008/05/21 17:38.$

The vector of global parameters $v_g$: $b_g = 3000; \ \sigma_g = 0.10; \ \gamma_g = 0.60; \ \hat{\sigma}_g = 0.05; \ \hat{\gamma}_g = 0.30; \ t_{mg} = 2008/01/16 10:45; \ t_{sg} = 2007/10/15 7:24; \ t_{eg} = 2008/04/19 14:07; \ f_T = 1$. Then, after maintenance the $KB_R$ will contain the following three rules: $p_1: \text{term\_architecture} \land \text{term\_schema} \Rightarrow \text{eval\_relevant} \ (sup = 0.12; \ con = 0.75; \ b = 3500; \ t_m = 2008/02/01 01:22)$, $p_2: \text{term\_copy} \land \text{term\_mechanism} \Rightarrow \text{stored\_yes}\ (sup = 0.21; \ con = 0.69; \ b = 3000; \ t_m = 2008/01/16 10:45)$, $p_3: \text{term\_schema} \Rightarrow \text{eval\_relevant} \ (sup = 0.15; \ con = 0.90; \ b = 500; \ t_m = 2008/05/05 17:04)$.

$term\_schema \Rightarrow eval\_relevant \ (sup = 0.15; \ con = 0.90; \ b = 500; \ t_m = 2008/05/05 17:04)$ and $r_2: \text{term\_base} \land \text{term\_matrix} \Rightarrow \text{eval\_relevant} \ (sup = 0.28; \ con = 0.85; \ b = 500; \ t_m = 2008/05/05 17:04)$. 

**Figure 4:** The transformed history while removing $N$ values (ENV algorithm).
stored\_yes (sup = 0.18; con = 0.67; b = 3500; t_m = 2008/02/01 01:22), and \( r_2 : \text{term\_base} \land \text{term\_matrix} \Rightarrow \text{eval\_relevant} \) (sup = 0.08; con = 0.44; b = 3500; t_m = 2008/02/01 01:22). The new values of the \( v_g \) vector will be: \( b_g = 3500; \sigma_g = 0.09; \gamma_g = 0.61; \bar{\sigma}_g = 0.05; \bar{\gamma}_g = 0.31; t_{mg} = 2008/02/01 01:22 \). At the end of the learning run all the analyzed \( KB_H \) facts are permanently removed from the history and the agent switches over from learning to performance mode.

5 Experimental results

The APS method was evaluated experimentally with respect to both qualitative and performance measures. For the experiments we used a synthetic T10.I5.D20K dataset, corresponding to the WWW browsing agent scenario, which was generated with the DataGen application [Dudek, 2005]. The dataset has the following parameters [Agrawal et al. 1994]: number of transactions \( |D| = 20000 \); mean transaction size \( |T| = 10 \); average size of maximal, potentially frequent itemsets \( |I| = 5 \); number of binary attributes 307. No facts inside the test dataset contain unknown values. While creating the data, the facts supporting rules (e.g. adaptive \& autonomous \& learning \( \Rightarrow \) relevant \& stored\_yes) were distributed uniformly within a period from 1 January 2004, 00:27:45 until 10 April 2005, 23:32:57 as an activity log of a hypothetical Internet user, who visited 20,000 pages in 465 days (about 15 months), which makes 43 pages daily on average. Experiments were conducted in two series in order to compare incremental and batch processing (see Figure 5). During every test run processing
time of particular APS steps (algorithms) was registered and after the run had been completed, the resulting rule base $KB_R$ was stored. Then we compared the rules discovered in the incremental and batch series, using the proposed qualitative measures: \textit{rule overlap}, \textit{supdiff} and \textit{condiff}, given below. The beneath \textit{rule overlapping ratio} is the percent share of rules with the same antecedents and consequents in the compared rule sets (ignoring possible differences in rule support or confidence).

$$\text{rule overlap}(R_1, R_2) = \frac{|KB_R^O(R_1, R_2)|}{|R_1| + |R_2| - |KB_R^O(R_1, R_2)|},$$

where $KB_R^O(R_1, R_2)$ is an intersection of two compared rule sets $R_1$ and $R_2$ with respect to syntactical equity of rules (see Definition 7). While \textit{rule overlap} is used to evaluate general accuracy of incremental mining, deeper insight is provided by the next two measures \textit{supdiff} and \textit{condiff}, which show how the rules mined incrementally differ from rules in the reference batch-mined set, regarding support and confidence.

$$\text{supdiff}(R_1, R_2) = \frac{1}{n} \left( \sum_{i=1}^{c} |\text{sup}(p_i) - \text{sup}(r_i)| + d \right),$$
$$\text{condiff}(R_1, R_2) = \frac{1}{n} \left( \sum_{i=1}^{c} |\text{con}(p_i) - \text{con}(r_i)| + d \right),$$

where $n$ is the number of all rules in $R_1$ and $R_2$ with different antecedents and consequents, $c = KB_R^O(R_1, R_2)$, $d = n - c$, and $p_i \in R_1$ has the same antecedent and consequent as $r_i \in R_2$ for $i \in \{1, \ldots, c\}$.

As the experimental testbed we used the \textit{APS Incremental Learning} application [Dudek et al. 2005, Dudek, 2005] running on an x86 machine with 892.50 MHz CPU, 752 MB SDRAM, 40 GB HDD, NTFS, under OS MS Windows 2000 Server. The program was implemented using MS Visual C++ .NET language and the database management system MS SQL Server 2000 Enterprise Edition. Inside the testbed environment we used the University of Helsinki implementation of the Apriori algorithm [Agrawal et al. 1994], developed by [Goethals, 2003], for mining association rules. The experiments were conducted with the following settings: $k = 1000$; $\sigma = 0.08$; $\gamma = 0.30$; $\hat{\sigma} = 0.04$ and $\hat{\gamma} = 0.15$.

The qualitative results proved perfect accuracy of the APS incremental rule discovery as compared to batch mining. The \textit{rule overlap} measure attained 100%, whereas \textit{supdiff} and \textit{condiff} were 0% for all examined runs. While this is what we can expect from incremental processing of the synthetic, uniform dataset T10.I5.D20K, less regular data (in real applications) is potentially a challenge for the APS method and it is likely to yield less accurate results. Yet, stable
rules (i.e. frequent, confident and appearing regularly) should be mined and maintained correctly, regardless the overall irregularity of a data set.

In the performance evaluation we compared processing time of the APS incremental learning (separating values for particular APS algorithms) to the time of batch rule mining. Analyzing the results we can see the high 60% workload share of rule base maintenance (the RMAIN algorithm), while sole association mining makes only 17%, similarly to filling the history schema (the HFILL algorithm). Other APS processing stages, such as selecting (FSEL), transforming the history schema (HTRANS) and fact deletion together scarcely take about 6% of time. While fact selection and deletion are indeed straightforward database operations, which can be very efficiently performed by contemporary database management systems, the HTRANS and ENV algorithms are more complex. Hence, the very small processing time share of HTRANS and ENV, which was observed, can be misleading in general. The former algorithm would certainly need more time, if the initial history schema contained more attributes (in our experiments there were only about 300). The ENV algorithm is even more complex $O(n^2 m)$, so it would work much longer for higher density of missing attribute values.

The overall APS processing time for subsequent fact blocks is quite stable, oscillating around the average value, while batch mining time grows roughly proportionally to the increasing number of analyzed facts (see Figure 6). The moment, when the APS outperforms batch mining (about 8000 for the T10.I5.D20K dataset), depends on application domain and analyzed data. But in general the
more APS learning runs are performed, the bigger profit in saving system resources (CPU, memory and disc space) is plausible.

6 Related work

There is hardly any research directly covering the contribution of this paper, but there are many works related to some parts and aspects of APS.

Firstly, there is a line of research exploring usage of data mining methods inside agent systems, including the Agent Academy (AA) by Symeonidis and his coworkers [Symeonidis et al. 2002]. AA uses data mining algorithms (such as ID3, C4.5 and Apriori) for training agents, based on a common knowledge repository. As compared to their system, the APS framework is an internal learning procedure of an autonomous agent and not an external training process, outside an agent.

Secondly, there are many works on web recommendation systems using various data mining techniques, such as: clustering, association rule mining, classifiers and decision trees. Yao, Hamilton and Wang [Yao et al. 2002] proposed the PagePrompter system, supporting web site administering by means of association rules and clusters, which are discovered through web log mining. Wang and Shao worked out a personalized recommendation method for e-learning students, based on analysis of past navigation sessions using clustering and association rules [Wang and Shao, 2004]. Within the same application domain, Chen, Hsieh and Hsu [Chen et al. 2007] used the Apriori algorithm inside the agent-based, personalized e-learning system (PELS) for mining association rules, which build the human learner’s profile and help to identify common misconceptions during the learning process. An interesting comparative study of sequential association rules, based on web log mining and used for building web document prediction models was done by Yang, Li and Wang [Yang et al. 2004]. In contrast to the above works, the proposed APS method is not restricted to the web recommendation domain (actually, it is only an example application), but it is a general learning framework for software agents.

Finally, many alternative methods of incremental association mining have been developed to date: FUP [Cheung et al. 1996], FUP<sub>2</sub> [Cheung et al. 1997], Borders [Aumann et al. 1999], MAAP [Zhou and Ezeife, 2001], SWF [Lee et al. 2005] and EDUA [Zhang et al. 2007]. However, they differ from the APS approach: (i) they use intermediate representation – frequent itemsets, while the APS operates on final rules, which are much more suitable for agent reasoning, (ii) they usually reduce, but do not eliminate reruns through analyzed data, while our method provides approximate results without any database rescanning (which allows reducing disc space usage); (iii) they mostly do not use any time decaying heuristics, whereas we proposed the $f_T$ time depreciation function.
in the APS. Data stream mining research uses concepts, which are very closely related to the idea of partial memory learning [Maloo and Michalski, 2004], developed in the APS. A good example is the estDec method of stream mining [Chang and Lee, 2003]. However, as compared to estDec, the APS method allows using a broader range of time decaying functions (not restricted to exponential decay) and it covers management of the whole data mining process, not only rule discovery and maintenance.

7 Conclusions

In this paper a novel APS method was proposed for incremental, statistical learning of software agents. The original contribution of this work is to incorporate into an agent architecture a complete data mining process, including data accumulation, selection and preprocessing, association rule mining, rule base maintenance and history flushing. The history transaction schema is transformed in every learning run, making the proposed method highly flexible, because different history attributes are allowed to appear in subsequent runs. The crucial part of the APS method is the RMAIN rule maintenance algorithm, which incrementally updates the agent’s rule base. RMAIN uses a time decaying function and it operates on rules, unlike most other incremental mining methods, which process only intermediate representation – frequent itemsets. Operating on rule level extends potential applications of APS beyond single-agent learning and enables fusing knowledge coming from the agent’s internal learning process with rules shared by other agents. As the analyzed history facts are disposed in every run of the learning cycle, in long-term perspective disk space and CPU time usage is reduced as compared to batch mining approach. This makes APS suitable for resource-bounded agents, which are supposed to work as tiny background processes, not disturbing user’s normal activity. The proposed learning method can be also beneficial, if an agent interlaces standard performance with stand-by periods, when it does not work toward any goal, but awaits new tasks from a user. Personal agents in the domain of web browsing, information retrieval and filtering are good examples of possible applications.

We verified experimentally the APS method using a uniform, synthetic web browsing scenario dataset. The tests proved perfect accuracy of the incrementally mined rules as compared to the reference rule sets, which were discovered in a batch mode. Based on these results we can conclude that the APS framework ensures good quality of incremental association rule mining and maintenance, provided that the fact data source is stable and does not change rapidly between subsequent learning runs. On the other hand, dynamic environments are expected to challenge the rule maintenance procedure, which can deteriorate qualitative results.
The APS framework is intended to be implemented as a learning module and integrated with existing agent architectures, which is an interesting issue for further research.

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